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Extending a MILP Compilation for Numeric Planning Problems

To Include Control Parameters

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Although PDDL is an expressive modelling language for planning problems, a significant limitation is imposed on the structure of actions: the parameters of actions are restricted to values from finite (in fact, explicitly enumerated) domains. In real-world, there are parameters whose values have infinite (or highly large-sized) domains, they are called control parameters. Thus, modelling and reasoning with these parameters is indeed a requirement. Recent work investigated planning with these parameters (Ivankovic et al. 2007). In this work, we are interested in MILP compilations, as control parameters can be easily modelled as additional variables of the model, whose values are only constrained by the actions preconditions, but not by the actions effects. We present here an extension of the MILP compilation of numeric planning problem with instantaneous actions, as control parameters can be easily modelled as additional variables of the model, whose values are only constrained by the actions preconditions, but not by the actions effects. We present here an extension of the MILP compilation of numeric planning problem with instantaneous actions (Piacentini et al. 2018) to include control parameters.

1 Problem Definition

Numeric planning introduces numeric state variables, extending planning tasks beyond the propositional formalism. We further extend the definition of numeric planning tasks by adding control parameters as follows.

Definition 1 A numeric planning task with control parameters is a tuple \((V_p, V_n, I, A, G)\), where:

- \(V_p\) is a finite set of propositional variables,
- \(V_n\) is a finite set of numeric variables,
- \(I\) is the initial state,
- \(A\) is a set of actions. Each action, \(a \in A\), is a tuple:
  - \(cparam(a)\) is a declaration of a finite set of numeric control parameters of action \(a\), where each \(d^a \in cparam(a)\) has a domain \((\text{dom}(d^a))\) of \(\mathbb{Q}\) or \(\mathbb{Z}\).
  - \(\text{pre}(a)\) is a set of preconditions. The preconditions can be propositional, \(\text{pre}_p(a)\), or numeric, \(\text{pre}_n(a)\). \(\forall p \in \text{pre}_p(a)\) corresponds to \(v_p \in V_p\) being true and \(\forall n \in \text{pre}_n(a)\) is of the form: \(\xi \geq 0\), where \(\xi \in \{\geq, >, =\}\) and \(\xi\) is a linear expression over \(V_n\) and \(cparam(a)\) with \(w^c, w^c_0 \in \mathbb{Q}\):
    \[
    \xi = \sum_{v \in V_n \cup cparam(a)} w^c v + w^c_0
    \]
  - \(\text{eff}(a)\) is a set of effects of the action \(a\), where it is defined as \(\text{eff}(a) = (\text{add}(a), \text{del}(a), \text{num}(a))\), with \(\text{add}(a)\) and \(\text{del}(a)\) are sets of added and deleted propositions, respectively. \(\text{num}(a)\) is a set of numeric effects that are assignments \(v := \xi\), where \(\xi\) is a linear expression over \(V_n\) and \(cparam(a)\) with \(k^a, k^c, k^c_0 \in \mathbb{Q}\):
    \[
    \xi = \sum_{w \in V_n \cup cparam(a)} k^a w + k^c_0
    \]
  - \(\text{cost}(a)\) is the cost of applying action \(a\).
- \(G\) is the goal described by a set of propositional, \(G_p\), and a set of numeric conditions, \(G_n\), over numeric variables.

A state is a mapping of each variable to its domain, where \(s(v)\) is the value of \(v\) in \(s\). An action \(a \in A\) is applicable in \(s\) iff \(s(v_p) = \text{true}, \forall v_p \in \text{pre}_p(a)\) and \(s(\xi) \geq 0\) for all numeric conditions of \(a\), where \(s(\xi)\) is the evaluation of \(\xi\) in \(s\). Given a state \(s\) and an applicable action \(a\), the successor state \(s'(s)\) is:
- \(\forall v_p \in V_p, s'(v_p) = \text{true}\) if \(v_p \in \text{add}(a), s'(v_p) = \text{false}\) if \(v_p \in \text{del}(a) \setminus \text{add}(a), s'(v_p) = s(v_p)\) otherwise. Each \(v_n \in V_n\) takes value \(s'(v_n) := s(\xi)\) if \((v_n := \xi) \in \text{num}(a)\), and \(s'(v_n) = s(v_n)\) otherwise.

A plan \(\pi\) is a sequence of actions and specified values for control parameters of actions in \(\pi\) (i.e. \(\pi = \{a_0, \text{eval}(a_0), \ldots, a_n, \text{eval}(a_n)\}\)), where \(n\) is the plan length, \(\text{eval}(a) \in \mathbb{Q}^m_n \cup \mathbb{Z}^m_n\) is the vector of values of the control parameters of \(a\), and \(m^a\) is the number of control parameters declared in action \(a\). In addition, all conditions of actions are met and the goals are satisfied in the final state.

The scope of each control parameter is restricted to its action. We use the PDDL language proposed by Savaş et al. (2016) to model our task, as it allows the declaration of multiple and typed (i.e. they can have integer or rational number domains) control parameters in the action schema. An example PDDL action encoding using this language is shown in Figure 1. The control parameters are declared in
the :control() field associated with their types.

((:action bake_a_cake
 :parameters (?c - spongecake)
 :control (?milk ?flour - number, ?cake - int)
 :precondition (and
   (>= ?milk ( 200 ?cake))
   (>= ?flour ( 100 ?cake)))
 :effect (and (increase (stock ?c) ?cake)))

Figure 1: An example PDDL action schema

2 MILP Formulation

In this section, we present the extension of the MILP formulation for numeric planning problem to handle control parameters. Due to space limitation, we report only the constraints necessary to model the numerical part of the problem. These constraints can be added to any of the MILP models designed for classical planning problems: the state-based model, the state-change model (Vossen et al. 1999) and the SAS+ state-change model (van den Briel, Vossen, and Kambhampati 2005).

Let $\mathcal{T} = \{0, ..., T - 1\}$ and $\bar{\mathcal{T}} = \mathcal{T} \cup \{T\}$ be sets of time-steps. Consider parameters $m_{a,t} \in \mathbb{Q}$, $\forall c \in C, \forall t \in \bar{\mathcal{T}}$, $M_{\text{step}}, m^a_{\text{step}}, M^a_{\text{t+1}}, m^a_{\text{t+1}} \in \mathbb{Q}$, $\forall v \in V_n \cup \{cparam(a)\}, \forall t \in \bar{\mathcal{T}}$, define as in previous work (Piacentini et al. 2018). Let $y_{v,c} \in Q \forall v \in V_n \cup \{cparam(a)\}, \forall t \in \bar{\mathcal{T}}$ represent the value of the numeric variable $v$ or the control parameter at time-step $t$. Variable $u_{a,t} \in \{0, 1\}$, $\forall a \in A, \forall t \in \bar{\mathcal{T}}$ indicates whether $a$ is applied at time-step $t$.

The constraints modelling numeric effects and conditions are given in Figure 2. Constraint (1) sets the variables to their initial state values, while constraint (2) enforces the numeric goal conditions. Constraints (3)-(7) update the values of the numeric variables according to the action effects (simple or linear). Constraints (8)-(9) model the effects of the actions on their control parameters. They become redundant if an action is not applied. Constraint (10) is added to model the type of the control parameters. Constraint (11) enforces the mutex relation, according to the numeric mutex relation presented in previous work (Piacentini et al. 2018).

3 Conclusion

Although most planning problems are efficiently solved using state space heuristic search approaches, they become highly cumbersome with the introduction of numeric parameters with large-sized domains. Constraint programming and operations research techniques are considerably powerful for these problems. We investigated only a small subset of the product of this cross-fertilisation between these fields, but the recent interest shows that it is ample.

References

[Fernández-González, Karpas, and Williams 2015]