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Abstract—We consider secure resource allocations for orthogonal frequency division multiple access two-way relay wireless sensor networks. The joint problem of subcarrier assignment, subcarrier pairing and power allocations is formulated under scenarios of using and not using cooperative jamming to maximize the secrecy sum rate subject to limited power budget at the relay station and orthogonal subcarrier allocation policies. The optimization problems are shown to be mixed integer programming and non-convex. For the scenario without cooperative jamming, we propose an asymptotically optimal algorithm based on the dual decomposition method, and a suboptimal algorithm with lower complexity. For the scenario with cooperative jamming, the resulting optimization problem is non-convex, and we propose a heuristic algorithm based on alternating optimization. Finally, the proposed schemes are evaluated by simulations and compared to the existing schemes.

Index Terms—Cooperative jamming, OFDMA, physical layer security, secure resource allocation, wireless sensor network.

I. INTRODUCTION

Wireless sensor networks (WSNs) play an important role in industrial monitoring and control [1] [2]. Relay node makes the WSN’s transmission more reliable to satisfy the strict requirements in industrial applications [3]. In the case that data from two wireless sensors are forwarded in opposite directions, two-way relay networks, in which sources exchange information through one assisting relay based on the idea of network coding, can make the bi-directional transmission more efficient [4]. In orthogonal frequency division multiple access (OFDMA) based two-way relay networks, channel gains of one subcarrier for one user differ from the other user, and system capacity can be maximized by subcarrier pairing, subcarrier allocation and power allocation [5]. Subcarrier pairing means the pairing of subcarriers in the two phases of two-way relay network. Subcarrier assignment means the allocation of subcarrier pairs to wireless sensor pairs. Power allocation means the power control of each subcarrier pair.

In order to achieve the multi-user diversity, subcarrier-pairing based resource allocation has been investigated in two-way relay systems [6]–[8], which optimize resource allocation using the Lagrange dual decomposition method. In [6], both rate and power allocation with subcarrier-user assignment were optimized based on the Lagrange dual decomposition method for a two-way relay network, while a multi-user system with a single relay was considered in [7]. Subcarrier-pairing based power allocation, subcarrier-pair assignment, and relay selection were jointly optimized in [8], where an asymptotically optimal algorithm was proposed based on a dual method.

Recently, physical layer security in terms of the secrecy capacity has drawn much attention due to the broadcast nature of wireless sensor communications [9] [10]. Compared to the traditional cryptography, physical layer security can strengthen secure transmission by taking full advantage of the additive nature of electromagnetic waves at low complexity [11]–[14].

Novel strategies have been explored to optimize secrecy capacity from either information-theoretic or signal processing approach. In [15], a resource allocation scheme was employed for OFDMA networks with coexistence of secure users and normal users, where the secure users have a minimum secrecy data rate requirement and the normal users are provided with best-effort services. Physical layer network coding (PNC) is an effective capacity boosting technique to improve throughput by embracing intrinsic interference in wireless channels [16]. In another popular scheme in the signal space of wiretap channel, cooperative jamming was studied in [17], [18].

Secure resource allocation and scheduling were investigated in half-duplex decode-and-forward (DF) relay assisted OFDMA networks [19], with the objective of maximizing average secrecy outage capacity by using artificial noise to combat a passive eavesdropper. In [20], power allocation for secrecy capacity maximization was studied in DF relay systems with the presence of an eavesdropper. In [21], secure resource allocation was investigated in two-way relay...

1The terms “user” and “sensor” are used interchangeably in this paper.
network. However, to the best of the authors’ knowledge, secure resource allocation jointly considering subcarrier-pairing, subcarrier assignment and power allocation in two-way relay wireless sensor networks without and with cooperative jamming (CJ) has not been studied in the literature.

In this paper, we investigate the secure resource allocation problem for an OFDMA two-way relay wireless sensor network in the presence of an eavesdropper with and without CJ. For the scenario without CJ, the joint optimization of subcarrier-pairing, subcarrier assignment and power allocation at the relay node is formulated as a mixed integer programming problem, which is then solved using the dual method in an asymptotically optimal manner. To reduce the complexity of the proposed resource allocation algorithm, we also propose a suboptimal algorithm. For the scenario with CJ, the resulting optimization problem is non-convex, and we propose a heuristic algorithm based on alternating optimization. Performance of the proposed schemes is verified by simulations.

The rest of the paper is organized as follows. Section II describes the system model without and with CJ. In Section III, the secure resource allocation problems without and with CJ are formulated. In Section IV, the secure resource allocation scheme without jamming is proposed by jointly considering subcarrier assignment, subcarrier pairing and power allocation based on the dual decomposition method, and a new suboptimal low-complexity algorithm is proposed. In Section V, we propose a suboptimal algorithm to solve the non-convex optimization problem of secure resource allocation with CJ. Section VI evaluates performance of the proposed algorithms by simulations. Finally, Section VII concludes the paper.

II. SYSTEM MODEL
A. Secrecy Two-Way Relay Wireless Sensor Networks without Cooperative Jamming

We consider an OFDMA based two-way relay wireless sensor network consisting of $M$ pre-assigned pairs of sensors, denoted by $M = \{1, \ldots, M\}$. These sensors aim to exchange information through the assistance of a fixed relay station (RS) in the presence of an eavesdropper (Eve) over an OFDMA channel composed of $N$ subcarriers (SCs), denoted by $N = \{1, \ldots, N\}$, each having a bandwidth $B$. As shown in Fig. 1, the system is composed of $M$ pairs of legitimate users. The only eavesdropper, denoted by $E$, is passive and attempts to overhear information from these wireless sensors. The RS operates in a half-duplex mode and relays the bi-directional traffic using the amplify-and-forward (AF) protocol, which is also known as analog network coding [22]. All wireless sensors, RS and eavesdropper are assumed to be equipped with a single omni-antenna.

The AF two-way relay wireless sensor transmission is divided into two phases: the multiple access (MA) phase and the broadcast (BC) phase. In the MA phase, all wireless sensors transmit signals to the RS simultaneously; in the BC phase, the RS amplifies and broadcasts the received signals to wireless sensors. In both phases, each subcarrier is occupied by no more than one wireless sensor pair in order to avoid the co-channel interference, while each wireless sensor-pair can occupy more than one subcarriers. The $m$th wireless sensor-pair is composed of wireless sensor $A_m$ and wireless sensor $B_m$, where $m \in M$.

We focus on the secure resource allocation including subcarrier-pairing, subcarrier assignment together with power allocation in the two-way relay wireless sensor system under the assumption that global channel state information (CSI) is known [15], [23] at the cooperative helper, RS. The fading channel on each of the subcarriers is assumed to be flat and composed of distance-dependent path loss and small scale fading. We consider a slow fading environment where all the channels are assumed to remain constant within the total transmission phase of our interest.

Assuming subcarrier $i$ is allocated to the $m$th wireless sensor pair in the MA phase, and the received signal at the RS on subcarrier $i$ can be expressed as

$$y_{RS,i} = \sqrt{P_{A_m,i}} h_{A_m,R,i} s_{A_m,i} + \sqrt{P_{B_m,i}} h_{B_m,R,i} s_{B_m,i} + n_{RS,i}$$

where $i \in N$; $s_{A_m,i}$ and $s_{B_m,i}$ are, respectively, the transmitted signals on subcarrier $i$ from wireless sensors $A_m$ and $B_m$, and are assumed to be cyclic symmetric complex Gaussian (CSCG) random variables denoted by $s_{A_m,i} \sim \mathcal{CN}(0,1)$ and $s_{B_m,i} \sim \mathcal{CN}(0,1)$, respectively; $P_{A_m}$ and $P_{B_m}$ are respectively the total transmit powers of $A_m$ and $B_m$ over all the available bandwidth; $h_{A_m,R,i}$ and $h_{B_m,R,i}$ are respectively the channel gains on subcarrier $i$ from $A_m$ to RS and from $B_m$ to RS; and $n_{RS,i}$ is the additive white Gaussian noise (AWGN) with mean zero and variance $\sigma^2$ at the RS on subcarrier $i$, and it is denoted by $n_{RS,i} \sim \mathcal{CN}(0, \sigma^2)$.

The received signal on subcarrier $i$ at the eavesdropper is given by

$$y_{E,i} = \sqrt{P_{A_m,i}} h_{A_m,E,i} s_{A_m,i} + \sqrt{P_{B_m,i}} h_{B_m,E,i} s_{B_m,i} + n_{E,i}$$

where $h_{A_m,E,i}$ and $h_{B_m,E,i}$ are the channel gains on subcarrier $i$ from $A_m$ to the eavesdropper and from $B_m$ to the eavesdropper, respectively; and $n_{E,i}$ is the AWGN at the eavesdropper on subcarrier $i$, and it is denoted by $n_{E,i} \sim \mathcal{CN}(0, \sigma^2)$.

Assuming subcarrier $j$ is allocated to the $m$th wireless sensor pair in the BC phase, the signal transmitted from the relay is given by $\beta_{m,i} y_{RS,i}$ and it is transmitted with power $P_{R,j}$.
on SC $j$, where $\beta_{m,i}$ is the amplifying coefficient, denoted by $\beta_{m,i} = \sqrt{P_{R,j}/\alpha_{m,i}}$, and where $\alpha_{m,i}$ is a normalized factor given by $\alpha_{m,i} = \sqrt{P_{A_m,i}[h_{A_m,R,i}^2 + P_{B_m,i}[h_{B_m,R,i}^2 + \sigma^2]$. We consider a total power constraint that limits the total transmit power at the RS over all SCs, i.e., $\sum_{j=1}^{N}P_{R,j} \leq P_R$.

The received signal at $A_m$ on subcarrier $j$ in the BC phase is thus $y_{A_m,i,j} = \sqrt{P_{R,j}g_{A_m,j}}y_{RS,i}/\alpha_{m,i} + n_{A_m,j}$, which can be further expressed as

$$y_{A_m,i,j} = \sqrt{P_{R,j}}g_{A_m,j}\sqrt{P_{A_m,i}h_{A_m,R,i}}s_{A_m,i}/\alpha_{m,i} + \sqrt{P_{R,j}g_{A_m,j}}\sqrt{P_{B_m,i}h_{B_m,R,i}}s_{B_m,i}/\alpha_{m,i} + \sqrt{P_{R,j}}g_{A_m,j}n_{RS,i}/\alpha_{m,i} + n_{A_m,j}.$$

Similarly, the received signal at $B_m$ on subcarrier $j$ is $y_{B_m,i,j} = \sqrt{P_{R,j}g_{B_m,j}}y_{RS,i}/\alpha_{m,i} + n_{B_m,j}$, which is further expressed as

$$y_{B_m,i,j} = \sqrt{P_{R,j}}g_{B_m,j}\sqrt{P_{A_m,i}h_{A_m,R,i}}s_{A_m,i}/\alpha_{m,i} + \sqrt{P_{R,j}g_{B_m,j}}\sqrt{P_{B_m,i}h_{B_m,R,i}}s_{B_m,i}/\alpha_{m,i} + \sqrt{P_{R,j}}g_{B_m,j}n_{RS,i}/\alpha_{m,i} + n_{B_m,j}.$$

where $g_{A_m,j}$ and $g_{B_m,j}$ are the channel gains from the RS to the $m$th user pair $A_m$ and $B_m$ on SC $j$, respectively; and $n_{A_m,j}$ and $n_{B_m,j}$ are AWGNs on subcarrier $j$ at $A_m$ and $B_m$, and they are denoted by $n_{A_m,j} \sim \mathcal{CN}(0, \sigma^2)$ and $n_{B_m,j} \sim \mathcal{CN}(0, \sigma^2)$, respectively.

The received signal on subcarrier $j$ at the eavesdropper in the BC phase is given by

$$y_{E,i,j} = \sqrt{P_{R,j}}g_{E,j}\sqrt{P_{A_m,i}h_{A_m,R_i}}s_{A_m,i}/\alpha_{m,i} + \sqrt{P_{R,j}g_{E,j}}\sqrt{P_{B_m,i}h_{B_m,R_i}}s_{B_m,i}/\alpha_{m,i} + \sqrt{P_{R,j}}g_{E,j}n_{RS,i}/\alpha_{m,i} + n_{E,j}.$$

where $g_{E,j}$ is the channel gain between the RS and the eavesdropper on SC $j$; and $n_{E,j}$ is the AWGN at the eavesdropper on subcarrier $j$, and it is denoted by $n_{E,j} \sim \mathcal{CN}(0, \sigma^2)$.

The signal-to-noise ratios (SNRs) of wireless sensors $A_m$ and $B_m$, which share subcarrier $i$ in the MA phase and subcarrier $j$ in the BC phase, can be respectively written as

$$SNR_{A_m,i,j} = \frac{P_{R,j}|g_{A_m,j}|^2P_{B_m,i}|h_{B_m,R_i}|^2/\alpha_{m,i}^2}{(P_{R,j}|g_{A_m,j}|^2/\alpha_{m,i}^2 + 1)\sigma^2}$$

and

$$SNR_{B_m,i,j} = \frac{P_{R,j}|g_{B_m,j}|^2P_{A_m,i}|h_{A_m,R_i}|^2/\alpha_{m,i}^2}{(P_{R,j}|g_{B_m,j}|^2/\alpha_{m,i}^2 + 1)\sigma^2}.$$

Based on (2) and (5), the composite received signal over the two phases at the eavesdropper can be modeled as a 2-by-2 point-to-point multiple-input-multiple-output (MIMO) channel given by

$$y_E = HEs + n_E$$

where

$$HE = \begin{bmatrix} \sqrt{P_{A_m,i}h_{A_m,E,i}}/\alpha_{m,i} & \sqrt{P_{B_m,i}h_{B_m,E,i}}/\alpha_{m,i} \\ \sqrt{P_{R,j}g_{A_m,j}P_{A_m,i}h_{A_m,R_i}}/\alpha_{m,i} & \sqrt{P_{R,j}g_{E,j}P_{B_m,i}h_{B_m,R_i}}/\alpha_{m,i} \end{bmatrix}.$$
For the eavesdropper, it receives a mixed signal on SC \( i \) expressed as

\[
y_E^{(1)} = \sqrt{1 - \alpha_A(i)} P_{A,m,i} h_{A,m,E,r} s_{A,m,i} + \sqrt{1 - \alpha_B(i)} P_{B,m,i} h_{B,m,E,r} s_{B,m,i} + \sqrt{\alpha_A(i)} P_{A,m,i} h_{A,m,E,r} s_{A,m,i} + \sqrt{\alpha_B(i)} P_{B,m,i} h_{B,m,E,r} s_{B,m,i} + n_{E,rs,i}. \tag{17}
\]

In this work, it is assumed that the AN signals, \( s_{A,m,i} \) and \( s_{B,m,i} \), are perfectly known to the RS prior to transmission via certain higher-layer cryptographic protocols, and as a result, at the RS, both \( \sqrt{\alpha_A(i)} P_{A,m,i} h_{A,m,E,r} s_{A,m,i} \) and \( \sqrt{\alpha_B(i)} P_{B,m,i} h_{B,m,E,r} s_{B,m,i} \) in (16) can be canceled [29] [30]. Thus, only \( s_{A,m,i} \) and \( s_{B,m,i} \) are broadcasted on SC \( j \) in the successive BC phase. Then, by means of analog network coding, \( A_m \) will be able to subtract \( s_{A,m} \) from the broadcast signal and obtain \( s_{B,m} \) as it desires, so will \( B_m \). However, since ANs are kept strictly confidential to the eavesdropper, it suffers from large interference caused by ANs and/or analog network coded signals containing both \( s_{A,m} \) and \( s_{B,m} \). Assuming the RS works in AF mode, it transmits the remaining signal after canceling \( s_{A,m} \) and \( s_{B,m} \), i.e., \( y_{RS,i} \), which is given by

\[
y_{RS,i} = \sqrt{1 - \alpha_A(i)} P_{A,m,i} h_{A,m,R,j} s_{A,m,i} + \sqrt{1 - \alpha_B(i)} P_{B,m,i} h_{B,m,R,j} s_{B,m,i} + n_{RS,i} \tag{18}
\]

with an amplifying coefficient denoted by \( \beta_{m,i} = \sqrt{P_{R,j}/|\gamma_{m,i}|} \) where

\[
|\gamma_{m,i}| = \sqrt{1 - \alpha_A(i) P_{A,m,i} h_{A,m,R,j}^2 + (1 - \alpha_B(i)) P_{B,m,i} h_{B,m,R,j}^2 + \sigma_i^2}. \tag{19}
\]

The parameter \( \gamma_{m,i} \) can be seen as a normalized factor for the forwarded signal, and thus \( P_{R,j} \) denotes the transmit power of the RS on SC \( j \) in the BC phase. Hence, the received signal at the \( A_m \) is given by

\[
y_{A,m,i,j} = \beta_{m,i} g_{R,A,m,j} y_{RS,i} + n_{A,m,j}. \tag{20}
\]

Note that since \( A_m \) can successfully cancel its previously transmitted \( s_{A,m} \) at its receiver, we can further simplify the received signal at the \( A_m \) by substituting \( \beta_{m,i} \) and \( y_{RS,i} \) into (19)

\[
y_{A,m,i,j} = \sqrt{1 - \alpha_B(i)} P_{R,j} P_{A,m,i} h_{A,m,R,j} g_{R,A,m,j} s_{B,m,i} + P_{R,j} g_{R,A,m,j} n_{RS,i} |\gamma_{m,i}| + n_{A,m,j}. \tag{21}
\]

Similarly, the received signal at the \( B_m \) is given by

\[
y_{B,m,i,j} = \sqrt{1 - \alpha_A(i)} P_{R,j} P_{A,m,i} h_{A,m,R,j} g_{R,B,m,j} s_{A,m,i} + P_{R,j} g_{R,B,m,j} n_{RS,i} |\gamma_{m,i}| + n_{B,m,j}. \tag{22}
\]

For the eavesdropper, since it does not know either \( s_{A,m,i} \) or \( s_{B,m,i} \), it receives a combined signal of \( s_{A,m,i} \) and \( s_{B,m,i} \), which is expressed as

\[
y_E^{(2)} = \sqrt{1 - \alpha_A(i)} P_{R,j} P_{A,m,i} h_{A,m,R,j} g_{R,E,i} s_{A,m,i} + P_{R,j} g_{R,E,i} n_{RS,i} |\gamma_{m,i}| + n_{E,j}. \tag{23}
\]

From (17) and (22), we can combine the received signals at the eavesdropper during the two phases in one transmit slot into an equivalent point-to-point 2-by-2 MIMO channel as

\[
y_E = \begin{bmatrix} y_E^{(1)} \\ y_E^{(2)} \end{bmatrix} = \begin{bmatrix} \tilde{h}_{11} \\ \tilde{h}_{12} \end{bmatrix} \begin{bmatrix} s_{A,m,i} \\ s_{B,m,i} \end{bmatrix} + \begin{bmatrix} \tilde{n}_1 \\ \tilde{n}_2 \end{bmatrix} \tag{24}
\]

where

\[
\tilde{h}_{11} = \sqrt{1 - \alpha_A(i)} P_{A,m,i} h_{A,m,E,r}, \quad \tilde{h}_{12} = \sqrt{1 - \alpha_B(i)} P_{B,m,i} h_{B,m,E,r}, \quad \tilde{h}_{21} = \sqrt{1 - \alpha_A(i)} P_{R,j} P_{A,m,i} h_{A,m,R,j} g_{R,E,i}, \quad \tilde{h}_{22} = \sqrt{1 - \alpha_B(i)} P_{R,j} P_{B,m,i} h_{B,m,R,j} g_{R,E,i}.
\]

For convenience, we denote the equivalent channel matrix from the wireless sensor pairs to the eavesdropper over the SC pair \((i, j)\)

\[
\tilde{H}_{E,m,i,j} = \begin{bmatrix} \tilde{h}_{11} & \tilde{h}_{12} \\ \tilde{h}_{21} & \tilde{h}_{22} \end{bmatrix} \tag{25}
\]

In (23), \( \tilde{n}_1 \) denotes the equivalent received noise at the eavesdropper treating the AN generated by the wireless sensor pair as noise in the MA phase, which is given by

\[
\tilde{n}_1 = \sqrt{1 - \alpha_A(i) P_{A,m,i} h_{A,m,E,r}^2 + \sqrt{1 - \alpha_B(i) P_{B,m,i} h_{B,m,E,r}^2 + \sigma_i^2}}.
\]

Similarly, \( \tilde{n}_2 \) denotes the amplified noise introduced by the RS as well as the additive noise received by the eavesdropper in BC phase, and it is given as

\[
\tilde{n}_2 = \sqrt{P_{R,j} g_{R,E,i} n_{RS,i} |\gamma_{m,i}} + n_{E,j}. \tag{26}
\]

The associated covariance matrix for this equivalent noise at the eavesdropper can thus be derived as

\[
\mathbf{Q}_{E,m,i,j} = \mathbb{E} \left[ \begin{bmatrix} \tilde{n}_1 \\ \tilde{n}_2 \end{bmatrix} \begin{bmatrix} \tilde{n}_1 & \tilde{n}_2 \end{bmatrix} \right] = \begin{bmatrix} \sigma_i^2 + \sigma_j^2 & \sigma_i \sigma_j \\ \sigma_i \sigma_j & \sigma_j^2 \end{bmatrix}.
\]

Besides, according to the received signal at \( A_m \) and \( B_m \) given by (20) and (21), the SNRs of wireless sensors \( A_m \) and \( B_m \), which share subcarrier \( i \) in the MA phase and subcarrier \( j \) in the BC phase, can be respectively expressed as

\[
SNR_{A,m,i,j} = \frac{(1 - \alpha_A(i) P_{R,j} P_{A,m,i} |g_{R,A,m,j}|^2 |h_{B,m,R,j}|^2 + \gamma_{m,i}^2)}{(P_{R,j} |g_{R,A,m,j}|^2 / \gamma_{m,i}^2 + 1) \sigma^2} \tag{27}
\]

and

\[
SNR_{B,m,i,j} = \frac{(1 - \alpha_A(i) P_{R,j} P_{A,m,i} |g_{R,B,m,j}|^2 |h_{A,m,R,j}|^2 + \gamma_{m,i}^2)}{(P_{R,j} |g_{R,B,m,j}|^2 / \gamma_{m,i}^2 + 1) \sigma^2} \tag{28}
\]

Similar to Section II-A without using CI, the IMI rate for the wireless sensor \( A_m \) and \( B_m \), are given by

\[
\tilde{R}_{A,m,i,j} = \frac{1}{2} B \log_2 (1 + SNR_{A,m,i,j}'), \tag{29}
\]

and

\[
\tilde{R}_{B,m,i,j} = \frac{1}{2} B \log_2 (1 + SNR_{B,m,i,j}'). \tag{30}
\]

respectively.
For the eavesdropper, since (23) is equivalent to a 2-by-2 point-to-point MIMO system with white transmission covariance denoted by $s \sim CN(0, I)$, where $s = (s_{A_{m,i}}, s_{B_{m,j}})^T$, the maximum achievable rate at the Eve is thus given by [28, Chap. 8]

$$
\hat{R}_{E,i,j} = \frac{1}{2} B \log_2 \det \left( I + \hat{H}_{E,m,i,j} \hat{H}_{E,m,i,j}^H \hat{Q}_{E,m,i,j}^{-1} \right).
$$

(32)

Accordingly, the worst-case secrecy sum rate using the scheme of CJ for the $m$th wireless sensor pair over the SC pair $(i, j)$ can be expressed as [27]

$$
\hat{R}_{\text{sec},m,i,j} = [\hat{R}_{A,m,i,j} + \hat{R}_{B,m,i,j} - \hat{R}_{E,i,j}]^+.
$$

(33)

III. SECURE RESOURCE ALLOCATION WITHOUT COOPERATIVE JAMMING

A. Proposed Problem without Cooperative Jamming

Our target is to maximize the total secrecy sum rate of the $M$ wireless sensor pairs by optimizing the subcarrier pairing, subcarrier assignment, and power allocations for the relay over different SCs. This optimization problem can thus be formulated as:

(P1): maximize \( \pi, \rho, P \)

subject to

\[
\begin{align*}
C1: & \quad \sum_{j=1}^{N} P_{R,j} \leq P_R, C2: P_{R,j} \geq 0, \forall j, \\
C3: & \quad \sum_{i=1}^{N} \pi_{i,j} \leq 1, \forall i, C4: \sum_{i=1}^{N} \sum_{j=1}^{N} \pi_{i,j} \leq 1, \forall j, \\
C5: & \quad \sum_{m=1}^{M} \rho_{m,(i,j)} \leq 1, \forall (i,j), \\
C6: & \quad \pi_{(i,j)}, \rho_{m,(i,j)} \in \{0,1\}, \forall m, i, j
\end{align*}
\]

(35)

where \( \pi = \{\pi_{(i,j)}\} \), \( \rho = \{\rho_{m,(i,j)}\} \), \( P = \{P_{R,j}\} \) for \( m \in M \), \( i, j \in N \). In order to ensure that each subcarrier pair \((i, j)\) is assigned to no more than one wireless sensor pair, we define the indicator of subcarrier allocation as \( \rho_{m,(i,j)} \in \{0,1\} \), where \( \rho_{m,(i,j)} = 1 \) if the $m$th wireless sensor pair occupies subcarrier $i$ in the MA phase and subcarrier $j$ in the BC phase; and \( \rho_{m,(i,j)} = 0 \) otherwise. Denote \( \pi_{(i,j)} \) as the subcarrier pairing variable such that \( \pi_{(i,j)} = 1 \) if subcarrier $i$ in the MA phase is paired with subcarrier $j$ in the BC phase, and \( \pi_{(i,j)} = 0 \) otherwise. Constraint C1 limits the total transmit power of the RS over all SCs; C2 represents the non-negative power constraint on each subcarrier; C3 and C4 guarantee that each subcarrier is paired with no more than one other subcarrier; C5 guarantees that each paired SCs can be assigned to at most one wireless sensor pair; and C6 indicates the integer property of \( \pi_{(i,j)} \) and \( \rho_{m,(i,j)} \).

The optimization problem defined in (34) under the constraints given in (35) is a non-convex integer-mixed optimization problem. According to [24], the duality gap between the primal problem and the dual problem approaches zero when the number of subcarriers is sufficiently large. In this section, we propose both near optimal and suboptimal schemes to solve the joint subcarrier pairing, subcarrier assignment and power allocations problem for the secrecy transmission in the OFDMA two-way relay wireless sensor networks using the Lagrange dual decomposition method [25] [26].

B. Near Optimal Algorithm to (P1)

The Lagrangian of (P1) is given by (36) on the top of next page. In (36), \( \lambda \) is the Lagrange multiplier (also called the dual variable) for the constraints $C1$ in (35) under the boundary constraints of $C3 \sim C6$ in (35). Accordingly, the Lagrange dual function is defined as

$$
g(\lambda) = \max_{\pi, \rho, P} L(\pi, \rho, P, \lambda).
$$

(37)

The dual problem can be expressed as

$$
\min_{\lambda} \ g(\lambda)
$$

subject to \( \lambda \geq 0 \).

(39)

We decompose the Lagrangian of (P1) in (36) into one master problem and $N$ subproblems with each of them corresponding to a different subcarrier $j$. Therefore, the Lagrangian in (36) is rewritten as

$$
L(\pi, \rho, P, \lambda) = \sum_{j=1}^{N} L_{j}(P_{R,j}, \pi_{(i,j)}, \rho_{m,(i,j)}, \lambda) + \lambda P_R \sum_{j=1}^{N} \pi_{(i,j)} \leq 1, \forall i, \forall j,
$$

$$
\sum_{i=1}^{N} \pi_{(i,j)} \leq 1, \forall j, \sum_{m=1}^{M} \rho_{m,(i,j)} \leq 1, \forall (i,j)
$$

and the associated subproblem can be formulated as

$$
\max_{\pi_{(i,j)}, \rho_{m,(i,j)}, P_{R,j}} \sum_{m=1}^{M} \sum_{i=1}^{N} \pi_{(i,j)} \rho_{m,(i,j)} R_{\text{sec},m,i,j} - \lambda P_{R,j}
$$

subject to \( \sum_{i=1}^{N} \pi_{(i,j)} \leq 1, \sum_{m=1}^{M} \rho_{m,(i,j)} \leq 1, \)

\( P_{R,j} \leq P_R. \)

(41)

Since \( L_{j}(P_{R,j}, \pi_{(i,j)}, \rho_{m,(i,j)}, \lambda) \) is an integer-mixed function and non-concave over \( P_{R,j} \), it cannot be solved directly. In the remaining of this section, we propose to jointly optimize \( P_{R,j}, \pi_{(i,j)} \), and \( \rho_{m,(i,j)} \) given \( \lambda \).

Firstly, providing that the subcarrier-pairing indicator \( \pi_{(i,j)} \) and the subcarrier assignment indicator \( \rho_{m,(i,j)} \) are given as \( \hat{\pi}_{(i,j)} \) and \( \hat{\rho}_{m,(i,j)} \), respectively, the objective is thus to maximize \( L_{j}(P_{R,j}, \hat{\pi}_{(i,j)}, \hat{\rho}_{m,(i,j)}, \lambda) \) over \( P_{R,j} \). Since \( L_{j}(P_{R,j}, \hat{\pi}_{(i,j)}, \hat{\rho}_{m,(i,j)}, \lambda) \) over \( P_{R,j} \) is still not concave over \( P_{R,j} \) but a continuous function over one single variable \( P_{R,j} \). We deploy the function \texttt{fmincon} in Matlab as \[ f_{\text{fmincon}} (P_{R,j}, \text{fval,exflag,output}) = \text{fmincon}(L_{j}, P_{R,j}^0, [], [], [], [], 0, P_R^2), \]\texttt{fmincon} denotes

2Function ‘fmincon’ is called in the syntax of: [x,fval,exitflag,output] = fmincon(fun,x0,A,b,Aeq,beq,l,ub) (c.f. doc ‘fmincon’ in MATLAB R2011b)
\[
L(\pi, \rho, \mathbf{P}, \lambda) = \sum_{m=1}^{M} \sum_{i=1}^{N} \sum_{j=1}^{N} \pi_{(i,j)} \rho_{m,(i,j)} P_{\text{sec},m,i,j} + \lambda \left( P_R - \sum_{j=1}^{N} P_{R,j} \right) \left| \sum_{j=1}^{N} \pi_{(i,j)} \leq 1, \forall i, \sum_{i=1}^{N} \pi_{(i,j)} \leq 1, \forall j, \sum_{m=1}^{M} \rho_{m,(i,j)} \leq 1, \forall (i,j) \right. (36)
\]

the near optimal solution and \textit{fval} the corresponding near optimal value, to solve the following problem

\[
\text{maximize } L_j(p_{R,j}, \hat{\pi}_{(i,j)}, \hat{\rho}_{m,(i,j)}, \lambda) \quad (42)
\]

subject to \quad \text{subject to } P_{R,j} \geq 0. \quad (43)

Next, we focus on finding the near optimal subcarrier pairing for (41). The subcarrier pairing problem can be equivalently transformed into an assignment problem and then solved by the classic Hungarian algorithm, where the assignment matrix consists of \(N \times N\) elements, with their index corresponding to the SC pair occupied during the phase of MA, and BC, respectively and with each entry a cost function given by

\[
c(\pi(i,j), \lambda) = R_{\text{sec},m,i,j} - \lambda \hat{P}_{R,j} \quad (44)
\]

where \(\hat{P}_{R,j}\) is given by the solution to (42) providing that \(\pi(i,j) = 1, \rho_{m,(i,j)} = 1\) and \(\hat{m} = \text{arg max}_{m} R_{\text{sec},m,i,j} - \lambda \hat{P}_{R,j}\). After filling in all entries, we denote the obtained near optimal subcarrier pairing policies via the Hungarian algorithm as \(\pi^*\).

At last, given the near optimal subcarrier pairing policies \(\pi^*\), the optimum subcarrier assignment for each pair of wireless sensors can be simultaneously given as

\[
\hat{\rho}_{m,(i,j)} = \begin{cases} 1 & \text{for } m = \hat{m}, \forall (i,j) \in \pi^*; \\ 0 & \text{otherwise}. \end{cases} \quad (45)
\]

We denote the near optimal subcarrier assignment as \(\rho^*\). Note that \(\hat{P}_{R,j}\) is already given when calculating (44).

Hence, given \(\lambda\), we can solve the corresponding \(P_{R,j}, \pi^*\) and \(\rho^*\) jointly for all \(j\). Problem (P1) is then iteratively solved by updating \(\lambda\) via a bisection method [25] given in Algorithm 1. The required sub-gradient for updating \(\lambda\) can be shown to be \(P_R - \sum_{j=1}^{N} P_{R,j}\) (c.f.(36)).

Algorithm 1 Proposed Algorithm to Solve (P1)

1: Initialize \(i = 0, \lambda_{\text{low}}^{(i)} = \lambda_{\text{min}}, \lambda_{\text{up}}^{(i)} = \lambda_{\text{max}}\);
2: repeat
3: \quad Update \(\lambda^{(i+1)} = (\lambda_{\text{low}}^{(i)} + \lambda_{\text{up}}^{(i)})/2\);
4: \quad \(i = i + 1\);
5: \quad Given \(\lambda^{(i)}\), update \(P_{R,j}^{(i)}\), \{\pi^{(i)}\} and \{\rho^{(i)}\} based on (44) and (45);
6: \quad Calculate the required sub-gradient: \(\text{subg}^{(i)} = P_R - \sum_{j=1}^{N} P_{R,j}^{(i)}\);
7: \quad if \text{subg}^{(i)} \geq 0; \lambda_{\text{up}}^{(i)} = \lambda^{(i)};
8: \quad \text{otherwise}, \lambda_{\text{low}}^{(i)} = \lambda^{(i)};
9: \text{until } |g(\lambda^{(i)}) - g(\lambda^{(i-1)})| < \epsilon, \text{ where } \epsilon \text{ is a small positive number that controls the algorithm accuracy.}

C. Suboptimal Algorithm to (P1)

The previous subsection gives a near-optimal resource allocation algorithm, the complexity of which may still be high with large values of \(M\) and \(N\). In this subsection, we propose a suboptimal algorithm to reduce the computational complexity by decomposing the joint optimization into three subproblems.

1) Subcarrier assignment for given power allocation and subcarrier pairing: We first allocate the power equally among all subcarriers, assuming the subcarrier pairing as \(\pi_{(i,j)} = 1, \rho_{m,(i,j)} = 0, \forall i \neq j\), that is, the same subcarrier is allocated to both MA and BC phases. Then the subcarrier pairing \(\pi_{(i,j)}\) is allocated to wireless sensor \(m\) according to:

\[
\hat{m} = \text{arg max}_m R_{\text{sec},m,i,j}, \forall i \quad (46)
\]

i.e., \(\rho_{\hat{m},(i,i)} = 1\). Then the SCs occupied by wireless sensor \(\hat{m}\) are denoted by the set \(\mathcal{S}_m = \{i | \rho_{m,(i,i)} = 1\}, \forall m \in \mathcal{M}\).

2) The subcarrier pairing schemes given equal power allocations over all SCs, and the obtained \(\mathcal{S}_m\)’s are given by Algorithm 2. Since the subcarrier pairing is not jointly optimized, it can be easily found that Algorithm 2 is suboptimal.

Algorithm 2 Suboptimal Subcarrier Pairing Algorithm for (P1)

1: Initialize \(k = 0, j^{(k)} = \emptyset\);
2: \(\forall m \in \mathcal{M}, \mathcal{S}_m = \mathcal{S}_m^*\);
3: repeat
4: \quad Set \(k = k + 1\); if \(\mathcal{S}_m \neq \emptyset\), randomly select an \(\hat{i} \in \mathcal{S}_m\), and choose \(j^{(k)} = \text{arg max}_j R_{\text{sec},m,i,j};\)
5: \quad \(\mathcal{S}_m = \mathcal{S}_m \setminus \{\hat{i}\}, \mathcal{S}_m = \mathcal{S}_m \setminus \{j^{(k)}\};\)
6: \text{until } \mathcal{S}_m \text{ (or } \mathcal{S}_m^* \text{) = } \emptyset\).

3) Given the subcarrier assignment and the subcarrier pairing schemes as stated in 1) and 2), the optimal power allocations can be obtained via calling the function \(f\text{mincon}\) as described in Section III-B.

The problem (P1) is thus solved iteratively by the same updating sub-gradient as stated in Section III-B via the bisection method [25].

D. Complexity Analysis

The total complexity of the proposed optimal algorithm is \(O(Y(\log Z NM^2 + N^3))\), where \(Y = \log_2(\frac{\lambda_{\text{max}} - \lambda_{\text{min}}}{\epsilon})\) is the number of iterations for implementing bi-section method given in Algorithm 1; \(Z\) is the complexity for the numerical
solver called by fmincon; \(ZM^2N^2\) is the number of arithmetic operations required to attain all the entries of the Hungarian assignment matrix, i.e., \(\{c(\pi(i,j),\lambda)\}_{i,j} \forall i \in \mathcal{N}, \forall j \in \mathcal{N}\); and \(N^3\) is the complexity for the classical Hungarian algorithm with \(N\) tasks and \(N\) workers. The proposed optimal scheme thus has a much lower complexity than the exhaustive search, which has a complexity of \(O(Y(2^N - 1)^MN!)\).

Similar analysis can be performed for the proposed suboptimal algorithm, and the complexity of which is \(O(Y(MN + \sum_{m=1}^{M} \frac{IS_m^2}{2} + Z))\), which is even lower than the proposed optimal algorithm.

IV. SECURE RESOURCE ALLOCATION WITH COOPERATIVE JAMMING

A. Proposed Problem with Cooperative Jamming

For the same problem with CJ, the objective function and constraints of the proposed resource allocation optimization can be modified as

\[
\text{(P1 - general)}: \quad \text{maximize} \quad \sum_{m=1}^{M} \sum_{i=1}^{N} \sum_{j=1}^{N} \tilde{\pi}(i,j) \tilde{\rho}_{m,(i,j)} \tilde{R}_{\text{sec},m,i,j} \quad (47)
\]

subject to

\[
C_1: \quad \sum_{j=1}^{N} \tilde{P}_{R,j} \leq P_R, \quad C_2: \quad \tilde{P}_{R,j} \geq 0, \forall j,
\]

\[
C_3: \quad \sum_{j=1}^{N} \tilde{\pi}(i,j) \leq 1, \forall i, \quad C_4: \quad \sum_{i=1}^{N} \tilde{\pi}(i,j) \leq 1, \forall j,
\]

\[
C_5: \quad \sum_{m=1}^{M} \tilde{\rho}_{m,(i,j)} \leq 1, \forall (i,j),
\]

\[
C_6: \quad \tilde{\pi}(i,j), \tilde{\rho}_{m,(i,j)} \in \{0,1\}, \forall m, i, j,
\]

\[
C_7: \quad 0 \leq \alpha_{1;i} \leq 1, 0 \leq \alpha_{2;i} \leq 1, \forall i,
\]

where \(\tilde{\pi} = \{\tilde{\pi}(i,j)\}, \tilde{\rho} = \{\tilde{\rho}_{m,(i,j)}\}, \tilde{P} = \{\tilde{P}_{R,j}\}\) for \(m \in \mathcal{M}, i, j \in \mathcal{N}\) are of the same meaning as those for problem (P1) but with different notation to represent variables of subcarrier and power allocations for the new problem with the scheme of CJ. Constraints \(C_3 \sim C_6\) have the same meaning as those of (35); \(C_7\) is the range constraint for variables denoting portions of the total transmit power allocated for AN at \(A_m\) and \(B_m\), respectively.

Similar to the secure resource allocation problem (P1) without CJ, the optimization problem (P1-general) is not a convex problem either since \(R_{\text{sec},m,i,j}\) is not concave over \(\alpha_{k,i}\) and/or \(P_{R,j}\), \(\forall i, j \in \mathcal{N}\) and \(k \in \{1,2\}\). The relationship between (P1-general) and (P1) can be seen as follows. When \(\alpha_{1;i} = 0, \alpha_{2;i} = 0\), problem (P1-general) reduces to problem (P1). It is easy to verify that, with \(\alpha_{1;i} = 0, \alpha_{2;i} = 0\), \(SNR_{A_{m,i,j}}^R\) and \(SNR_{B_{m,i,j}}^R\) in (28) and (29) can be simplified into \(SNR_{A_{m,i,j}}\) and \(SNR_{B_{m,i,j}}\) in (6) and (7), respectively. In addition, eqs. (24) and (27) also reduce to (9) and (14), respectively. Therefore, problem (P1-general) with CJ is a general case of problem (P1).

B. Proposed suboptimal Algorithm to (P1-general)

Similar to (P1), (P1-general) can be decomposed into parallel subproblems for each SC. The subproblem for SC \(j\) is

\[
\text{maximize} \quad \sum_{m=1}^{M} \sum_{i=1}^{N} \bar{\pi}(i,j) \bar{\rho}_{m,(i,j)} \bar{R}_{\text{sec},m,i,j} - \lambda P_{R,j} \quad \text{subject to} \quad \sum_{i=1}^{N} \bar{\pi}(i,j) \leq 1, \sum_{m=1}^{M} \bar{\rho}_{m,(i,j)} \leq 1, 0 \leq \alpha_{1;i} \leq 1, 0 \leq \alpha_{2;i} \leq 1, P_{R,j} \leq P_R. \quad (49)
\]

Since (49) is an integer-mixed function and non-concave over \(P_{R,j}\) and/or \(\alpha_{k,i}, k \in \{1,2\}\), (P1-general) is challenging to solve in general, and thus we propose to solve it via alternating optimization over \(\alpha_{k,i}, \forall k \in \{1,2\}, \forall i \in \mathcal{N}\). Substitute the optimal \(\pi^*, \rho^*\) and \(P^*\) to problem (P1) into (P1-general). Then, for each \(j\), since the corresponding \(i\) is already given as \(i = \arg \pi^*(i,j)\), eq. (49) can be simplified into

\[
\text{maximize} \quad \bar{R}_{\text{sec},m,i,j} \quad \text{subject to} \quad 0 \leq \alpha_{1;i} \leq 1, 0 \leq \alpha_{2;i} \leq 1. \quad (50)
\]

However, since (50) is still not a convex problem due to its non-concavity over \(\alpha_{1;i}\) and/or \(\alpha_{2;i}\), we first fix \(\alpha_{1;i} = \bar{\alpha}_{1;i}\) and optimize \(\alpha_{2;i}\) by solving the following problem

\[
\text{(P1 - general - sub1)}: \quad \text{maximize} \quad \bar{R}_{\text{sec},m,i,j} \quad \text{subject to} \quad 0 \leq \alpha_{2;i} \leq 1.
\]

Let the optimal solution to (P2-general-sub1) be denoted by \(\bar{\alpha}_{2;i}\), we optimize \(\alpha_{1;i}\) by fixing \(\alpha_{2;i} = \bar{\alpha}_{2;i}\) and solve a symmetric problem as follows

\[
\text{(P1 - general - sub2)}: \quad \text{maximize} \quad \bar{R}_{\text{sec},m,i,j} \quad \text{subject to} \quad 0 \leq \alpha_{1;i} \leq 1.
\]

Problem (P1-general-sub1), despite of non-convexity, can be easily solved via a one-dimensional search over \(\alpha_{2;j} \in [0,1]\). Similar method can be applied to solving (P1-general-sub2).

Since alternatively solving (P1-general-sub1) and (P2-general-sub2) guarantees the secrecy sum rate \(\bar{R}_{\text{sec},m,i,j}\) in (50) is non-decreasing after each iteration, it at least converges to a local optimum solution to (50). Together with \(\pi^*(i,j), \rho^*_{m,(i,j)}\) and \(P^*_R\), we find a suboptimal solution to (50).

Moreover, as \(\alpha_{1;i}\) and \(\alpha_{2;i}\) are independent over \(i\)’s, problem (P1-general) can finally be solved by state over all \(j\)’s. (Note that \(i\)’s and \(j\)’s compose a one-to-one correspondence after implementing Algorithm 1 in Section III-B.) Next, denote the optimal power portion factors for generating AN given \(\pi^*, \rho^*\) and \(P^*\) as \(\alpha^*_{1;i}\)’s and \(\alpha^*_{2;i}\)’s, we further optimize (P1-general) by fixing \(\alpha^*_{1;i}\)’s and \(\alpha^*_{2;i}\)’s as follows.

By decomposing (P1-general) into parallel subproblems, each for one SC \(j\) \(\left(\forall j \in \mathcal{N}\right)\), the modified subproblem for
(P1-general) can be expressed as

\[
\text{maximize} \quad \sum_{m=1}^{M} \sum_{i=1}^{N} \bar{\pi}(i,j) \rho_{m,(i,j)} \tilde{R}_{\text{sec},m,i,j} - \lambda \tilde{P}_{R,j}
\]

subject to \( \sum_{i=1}^{N} \bar{\pi}(i,j) \leq 1, \quad \sum_{m=1}^{M} \rho_{m,(i,j)} \leq 1, \quad \tilde{P}_{R,j} \leq P_{R} \). \quad (51)

Then, similar procedure to that of problem (41) can be taken to solve (51). Therefore, given \( \alpha_{1,i}^* \)'s and \( \alpha_{2,i}^* \)'s, problem (P1-general) can also be approximately solved by the Lagrangian dual decomposition method due to the same reason as that for (P1). The overall suboptimal algorithm for solving (P1-general) is summarized in Algorithm 3.

Algorithm 3 Proposed Suboptimal Algorithm to Solve (P1-general)

1. Denote optimal solution to (P1) as \( \pi^*, \rho^* \) and \( P^* \);
2. Initialize \( \pi = \pi^*, \rho = \rho^*, \) \( P = P^*, \) \( j = 0 \);
3. repeat
4. Set \( j = j + 1 \) and Initialize \( k = 0, \alpha_{1,i}^{(k)} = 0.5 \), where \( i = \text{arg} \pi^*(i,j) \);
   a. Set \( k = k + 1 \);
   b. with \( \tilde{\alpha}_{1,i} = \alpha_{1,i}^{(k-1)} \), obtain \( \alpha_{1,i}^{(k)} \) by solving (P1-general-sub1);
   c. with \( \tilde{\alpha}_{2,i} = \alpha_{2,i}^{(k)} \), obtain \( \alpha_{1,i}^{(k)} \) by solving (P1-general-sub2);
   d. Update \( \tilde{R}_{\text{sec},m,i,j}^{(k)} \);
   e. Until \( |\tilde{R}_{\text{sec},m,i,j}^{(k)} - \tilde{R}_{\text{sec},m,i,j}^{(k-1)}| \leq \epsilon \), where \( \epsilon \) is a small positive number that controls the algorithm accuracy.
   f. Denote final \( \alpha_{1,i}^{(k)} \)'s and \( \alpha_{2,i}^{(k)} \)'s, as \( \alpha_{1,i}^* \) and \( \alpha_{2,i}^* \), respectively.
5. until \( j = N \).
6. Solve (P1-general) given \( \{\alpha_{1,i}^*\} \) and \( \{\alpha_{2,i}^*\} \) based on Algorithm 1.

C. Complexity Analysis

The complexity of the proposed suboptimal algorithm is \( O(NX + Y(ZMN^2 + N^2)) \), where \( X \) is the number of arithmetic operations required for conducting alternating optimization including (P1-general-sub1) and (P1-general-sub2). Since (P1-general) contains three continuous variables, i.e., \( \alpha_{1,i}, \alpha_{2,i}, \) and \( \tilde{P}_{R,j} \), which are coupled together besides integer variables, i.e., \( \tilde{\pi}(i,j) \) and \( \tilde{\rho}_{m,(i,j)} \) for subcarrier allocations. It is computationally expensive for exhaustive search over the feasible region without complexity-friendly heuristic algorithms such as the one proposed in Algorithm 3.

V. SIMULATION RESULTS AND DISCUSSION

Simulation results are given in this section to evaluate the performance of the proposed resource allocation algorithms. Figs. 2-5 are the results of secure resource allocation without jamming, and Figs. 6-8 are the results of secure resource allocation with cooperative jamming. Legitimate users are distributed evenly along a circle around the central RS with a radius of 30 m. Except for the simulation in Fig. 2, the eavesdropper is assumed to be located at a distance of \( d = 200 \) m from the RS. The total transmit power for each wireless sensor is \( P_{Am}(P_{Bm}) = 300 \) mW for Fig. 2, Fig. 3 and Fig. 5. The carrier frequency is 2 GHz and the noise power is \( \sigma^2 = BN_0 \), where \( B = 150 \) kHz is the bandwidth of each subcarrier and \( N_0 = 10^{-21} \) mW/Hz is the AWGN power spectral density.

Unless otherwise specified, there are \( N = 32 \) subcarriers assumed in the OFDMA two-way relay wireless sensor network. The path loss exponent is 3. The number of wireless sensor pairs is fixed at 3 if not specified otherwise. There exists only one eavesdropper. The multi-path channel fading coefficients are modeled as independent and identically distributed (i.i.d.) Rayleigh distributed random variables.

Figure 2 illustrates the secrecy sum rate of both near optimal and suboptimal algorithms of P1 for different number of legitimate wireless sensor pairs assuming that a potential eavesdropper may exist at a distance between 150 m and 500 m from the RS. In Figs. 2-5, “near optimal” refers to the near optimal algorithm proposed for P1 in Subsection IV. A, and “suboptimal optimal” refers to the suboptimal algorithm proposed for P1 in Subsection IV. B. We can see that the secrecy sum rate increases when the eavesdropper moves further away from the RS, in particular, when the eavesdropper departs from the relay at a distance within 200 m, because pathloss is a major factor deteriorating the received signal of the eavesdropper. The secrecy sum rate approaches a relatively stable level when the eavesdropper is away from the RS for more than 500 m. Meanwhile, the suboptimal algorithm performs worse than the near optimal scheme.

Figure 3 shows the secrecy sum rate of the first two proposed algorithms of P1 versus the total transmit power of the RS for 3, 7, and 11 pairs of legitimate wireless sensors. It can be observed that the secrecy sum rate grows with an increase of the transmit power of the RS. In our proposed power allocation algorithm, the transferred Lagrange dual problem is solved by Algorithm 1, which results in a \( 32 \times 1 \) vector \( P \) containing optimal power in each subcarrier. This solution (33) demonstrates that in a specified \( \tilde{P}_{R} \), the sum of entries in the vector always equals \( \tilde{P}_{R} \). That means the
Secrecy capacity versus optimal and suboptimal algorithms for $P_1$ in terms of the transmit power of each legitimate user for higher secrecy sum rate will be obtained with more transmit power of the RS is thoroughly allocated. Therefore, secrecy sum rate converges to its optimal value when the total transmit power of the RS is set. In Fig. 5, the equal (P1) scheme is composed of subcarrier pairing and assignment scheme, where

$$\text{M} = 7, \quad \text{M} = 11$$

is set. In Fig. 5, the equal (P1) scheme is Algorithm 3 with equal power allocation based secrecy sum rate of the two-way relay wireless sensor system versus $P_{A,m}/\sigma^2$ for different values of $N$. The RS has a fixed total transmit power of 600 mW over all subcarriers. The system sum rate goes up sharply with an increase of the SNR of wireless sensor at each subcarrier, while the secrecy sum rate increases at a relatively lower rate because of those information leaked to the eavesdropper. Fig. 6 demonstrates that in a secrecy sensitive two-way relay wireless sensor system, the secrecy sum rate is remarkably deteriorated due to the potential leaked data rate to an eavesdropper. Particularly, in a system with a higher SNR of legitimate wireless sensors, leaked rate to the eavesdropper gets larger as well, which can be seen from the difference between the two curves of the same $N$. Obviously, when diversity gains in an OFDMA system increase with number of subcarriers $N$, the system leaked rate also enlarges.

Figure 7 shows improved performance of the proposed near optimal and suboptimal algorithms for $P_1$ in terms of the secrecy capacity versus $P_R$, compared to the equal power allocation scheme, where $M = 7$ is set. In Fig. 5, the equal (P1) scheme is composed of subcarrier pairing and assignment discussed in Part A of Subsection IV, and an equal power allocation across all subcarriers.
The system secrecy sum rate obtained from the proposed suboptimal Algorithm 3 grows fast for $P_{Am,i}/\sigma^2$ between 20 dB and 35 dB, and less so fast after $P_{Am,i}/\sigma^2$ reaches 40 dB. The proposed Algorithm 3 thoroughly outperforms the equal (P1-general) scheme. However, under scenarios with less subcarriers, the difference between them is obviously smaller due to the less diversity gains over subcarriers. It shows that the proposed Algorithm 3 performs to its full advantage at a medium to high range of $P_{Am,i}/\sigma^2$ in OFDMA systems, which is reasonable in practical systems.

Figure 8 shows the improved performance of the proposed Algorithm 3 versus $P_{R;j}/\sigma^2$ over each individual carrier $j$ ($k$), when compared to the equal (P1-general) scheme and the near optimal scheme in P1, for $N = 48$, and $N = 64$, where the transmit power of wireless sensors is fixed at 100 mW over all subcarriers. It can be observed that the secrecy sum rate in the system deploying the proposed Algorithm 3 increases with the increasing of $P_{R;j}/\sigma^2$. The selected working mode of the RS, i.e., AF, can account for the fast growing secrecy sum rate of the two-way relay wireless sensor system, which closely depends on the transmit power at the RS in the BC phase. We can also find that when $N$ becomes larger, the proposed Algorithm 3 outperforms more significantly than the equal (P1-general) scheme. Compared to cases with increased $P_{Am,i}/\sigma^2$ of wireless sensor, increased $P_{R;j}/\sigma^2$ is shown to make more advantage of the proposed Algorithm 3. It also makes sense that in practical systems, larger $P_{R;j}/\sigma^2$ of the central RS is easier to be realized than larger $P_{Am,i}/\sigma^2$ of every distributed wireless sensors. As shown in Fig. 8, CJ enabled Algorithm 3 outperforms the near optimal scheme for P1 without CJ.

VI. CONCLUSION

In this paper, we investigated the joint subcarrier pairing, subcarrier allocation and power allocation for secure two-way relay wireless sensor network in the presence of an eavesdropper without and with cooperative jamming. In the scenario without cooperative jamming, the proposed near optimal resource allocation algorithm properly allocates resources to wireless sensors, and the performance of secrecy sum rate of the system can be significantly improved. Moreover, a suboptimal algorithm was proposed to reduce the computational complexity. In the other scenario, a cooperative jamming scheme agreed by each pair of wireless sensors was proposed to confuse the eavesdropper while keeping the RS informed. Simulation results were presented to show the effectiveness of the proposed algorithms. In the future, we will extend this work to multi eavesdrover and imperfect channel knowledge scenarios [31].

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