Estimating mobility using sparse data: Application to human genetic variation

Liisa Loog\textsuperscript{a,b,c,d,1}, Marta Mirazón Lahr*\textsuperscript{e}, Mirna Kovacevic\textsuperscript{a,f}, Andrea Manica\textsuperscript{g}, Anders Eriksson\textsuperscript{h}, and Mark G. Thomas\textsuperscript{a,i}

\textsuperscript{a}Research Department of Genetics, Evolution and Environment, University College London, London WC1E 6BT, United Kingdom; \textsuperscript{b}Research Laboratory for Archaeology & the History of Art, University of Oxford, Oxford OX1 3QY, United Kingdom; \textsuperscript{c}Department of Zoology, University of Cambridge, Cambridge CB2 3EJ, United Kingdom; \textsuperscript{d}Manchester Institute of Biotechnology, School of Earth and Environmental Sciences, University of Manchester, Manchester M1 7DN, United Kingdom; \textsuperscript{e}Vehemence Centre for Human Evolutionary Studies, Department of Archaeology and Anthropology, University of Cambridge, Cambridge CB2 1QH, United Kingdom; \textsuperscript{f}Centre for Mathematics and Physics in the Life Sciences and Experimental Biology, University College London, London WC1E 6BT, United Kingdom; and \textsuperscript{g}Department of Medical and Molecular Genetics, King’s College London, London SE1 9RT, United Kingdom

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Mobility is one of the most important processes shaping spatiotemporal patterns of variation in genetic, morphological, and cultural traits. However, current approaches for inferring past migration episodes in the fields of archaeology and population genetics lack either temporal resolution or formal quantification of the underlying mobility, are poorly suited to spatially and temporally sparsely sampled data, and permit only limited systematic comparison between different time periods or geographic regions. Here we present an estimator of past mobility that addresses these issues by explicitly linking trait differentiation in space and time. We demonstrate the efficacy of this estimator using spatiotemporally explicit simulations and apply it to a large set of ancient genomic data from Western Eurasia. We identify a sequence of changes in human mobility from the Late Pleistocene to the Iron Age. We find that mobility among European Holocene farmers was significantly higher than among European hunter–gatherers both pre- and postdating the Last Glacial Maximum. We also infer that this Holocene rise in mobility occurred in at least three distinct stages: the first centering on the well-known population expansion at the beginning of the Neolithic, and the second and third centering on the beginning of the Bronze Age and the late Iron Age, respectively. These findings suggest a strong link between technological change and human mobility in Holocene Western Eurasia and demonstrate the utility of this framework for exploring changes in mobility through space and time.

Significance

Migratory activity is a critical factor in shaping processes of biological and cultural change through time. We introduce a method to estimate changes in underlying migratory activity that can be applied to genetic, morphological, or cultural data and is well-suited to samples that are sparsely distributed in space and through time. By applying this method to ancient genome data, we infer a number of changes in human mobility in Western Eurasia, including higher mobility in pre- than post-Last Glacial Maximum hunter–gatherers, and oscillations in Holocene mobility with peaks centering on the Neolithic transition and the beginnings of the Bronze Age and the Late Iron Age.

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Data deposition: The R code used for analyses is available from the GitHub repository (https://github.com/LiisaLoog/SpaceTime-Framework.git).

To whom correspondence may be addressed. Email: Liisa.Loog@gmail.com or m.thomas@ucl.ac.uk.

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One of the major goals of population history inference is to assess the role played by past mobility in shaping patterns of genetic, phenotypic, and cultural variation. It is well recognized that the past movement of people shapes geographic patterns of genetic variation (1) and the subsequent ecological and evolutionary properties of populations (2). This is due to the fact that gene flow changes allele frequencies, shapes genetic drift, and can affect (3) or even mimic (4) natural selection processes. It is also recognized that migration activity can influence cultural evolutionary processes (5, 6). However, despite the general agreement that mobility has played an important role in shaping past and present patterns of genetic, phenotypic, and cultural variation among humans, relatively little is known about its temporal and geographic variation in the past (7).

Inferring past mobility is challenged by the sparseness and unevenness of sampling in time and space. As a result, studies of prehistorical mobility are typically limited to descriptive approaches, where major attested migration episodes or events are used as a proxy for general mobility. Data sources such as stable isotopes have enabled some quantification of mobility by allowing researchers to identify individuals within an archaeological community who have migrated into a region during their lifetime (e.g., ref. 8). The underlying logic behind this approach is that differences between isotope ratios—particularly strontium—within organisms reflect the isotope ratios acquired from the local environment (as a result of variation in underlying geology) (9). However, it is challenging to extrapolate within-community mobility rates to migration rates across larger geographic regions or over long time periods. Furthermore, isoscapes are still often poorly characterized, and isotope ratios can be relatively constant over large areas (9, 10) and so are not always informative.

Most standard population genetic tools used for quantifying population structure, such as ADMIXTURE analysis (11), f statistics (12), and TREEMIX (11), are poorly suited for estimating underlying mobility change through time. In classical population genetic analysis, estimators of migration rates between hypothesized subpopulations have been developed, including statistics such as $F_{ST}$ (13). Some of these statistics have also been applied to large sets of quantitative trait data, such as variation in craniometric morphology (e.g., refs. 14 and 15). However, such statistics quantify differentiation among a set of contemporaneous samples and only inform on migration rates under idealized demographic scenarios—such as gene flow between discrete subpopulations—and are also influenced by other factors, such as subpopulation split times and population size fluctuations. Furthermore, these estimators reflect past migration between hypothesized subpopulations over large periods of time and therefore lack temporal resolution. Some researchers interpret the estimated ages and geographic distribution of clades on a phylogenetic tree of uniparental genetic systems as reflecting the underlying mobility, are poorly suited to spatially and temporally sparsely sampled data, and permit only limited systematic comparison between different time periods or geographic regions. Here we present an estimator of past mobility that addresses these issues by explicitly linking trait differentiation in space and time. We demonstrate the efficacy of this estimator using spatiotemporally explicit simulations and apply it to a large set of ancient genomic data from Western Eurasia. We identify a sequence of changes in human mobility from the Late Pleistocene to the Iron Age. We find that mobility among European Holocene farmers was significantly higher than among European hunter–gatherers both pre- and postdating the Last Glacial Maximum. We also infer that this Holocene rise in mobility occurred in at least three distinct stages: the first centering on the well-known population expansion at the beginning of the Neolithic, and the second and third centering on the beginning of the Bronze Age and the late Iron Age, respectively. These findings suggest a strong link between technological change and human mobility in Holocene Western Eurasia and demonstrate the utility of this framework for exploring changes in mobility through space and time.

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(mtDNA or the Y chromosome) as proxies for the rate of spread of populations (e.g., ref. 16). However, such approaches do not permit a formal quantification of mobility and have been criticized as a tool for demographic inference (17–19).

Thus, existing methods allow us to identify migration episodes to some extent but lack the temporal resolution and formal quantification of underlying mobility, are poorly suited to spatially and temporarily sparsely sampled data, and do not permit systematic comparison between different time periods or geographic regions. To overcome these problems, we present an estimator of past mobility that is particularly suited to sparsely distributed morphological, cultural, or genetic variation data and provide a first application to a large set of genome-wide data from ancient individuals from across Western Eurasia. We define mobility as the average distance moved by entities in a given time period.

### Estimating Past Migration Rates

Under a general model of identity-by-descent with modification and isolation by distance (IBD) (20, 21), trait (genetic, morphological, or cultural) differences between any two entities (individuals or populations) increase monotonically as a function of both the temporal and spatial distance between them. We therefore expect that trait differences between entities correlate with temporal as well as spatial distances. However, the extent to which spatial and temporal differences explain observed trait variation depends on the level of spatial population structure and therefore on the level of mobility. If mobility was low (i.e., strong spatial structure), then we would expect differences between entities to be more strongly correlated with space, relative to time, whereas if mobility was high we would expect time to explain a relatively larger proportion of differences between entities (because of the homogenizing effects of high mobility across space).

Given that both spatial and temporal distances are expected to correlate with trait differences among entities, a matrix combining both spatial and temporal distance information should give a stronger correlation than either matrix alone (extra correlation, EC). However, since spatial and temporal distances are measured in different units (e.g., kilometers and years), combining them requires a scaling factor ($S$). Here, we show that the scaling factor value ($S_{\text{max}}$) that maximizes the correlation between a trait difference matrix and a Euclidean distance matrix combining the spatial and temporal distance matrices provides an estimator of mobility over the period and region covered by the data (see Materials and Methods and Fig. 1). For convenience, we use a geometric interpretation of the scaling factor $S_{\text{max}}$, as an angle, $\alpha$, in the plane defined by the spatial and temporal distances [$\alpha = \tan^{-1}(S_{\text{max}})$, illustrated in Fig. 1, Inset; see Materials and Methods].

To test the reliability and the robustness of $S_{\text{max}}$ in recovering information about past mobility, we simulated data under a spatiotemporally explicit 2D model, which includes simple population dynamics with population growth, density dependence, and mobility (modeled as a Gaussian random walk), and generated variation data under different mobility parameter values (see Materials and Methods). We assessed the ability of $S_{\text{max}}$ to infer simulated mobility values by correlation across simulations. We found a strong, positive linear relationship between the simulated average migration distance (i.e., mobility) and values of $S_{\text{max}}$ (Fig. 2; $R^2 = 0.8$), thus demonstrating the utility of this statistic as an estimator for relative mobility. However, for this result to hold, it is important that the trait differences are generated under an approximately constant mutation rate and vary neutrally within a population.

### Migration Rates Among Pleistocene Hunter–Gatherers and Early Farmers

Recent advances in sequencing technologies have allowed genomic data retrieval from a large sample of past individuals (e.g., refs. 22–26). Although these studies have not explicitly quantified underlying mobility in the past, they have suggested several periods of large-scale population turnover in Western Eurasia. Given that the $S_{\text{max}}$ statistic is able to recover information on past mobility in simulated data, we applied the method to a sample (n = 329) of previously published genome-wide genotype data covering a time period from the beginning of the Upper Paleolithic to the Iron Age to explore changes in past human mobility in Western Eurasia (see Materials and Methods). We also constructed nonparametric confidence intervals to account for date and sampling uncertainty and estimated $P$ values for the $S_{\text{max}}$ statistic by permutation under the null hypothesis of no IBD in space and time, which allowed us to quantify the robustness of our estimates and identify time periods during which data are too sparse for the $S_{\text{max}}$ statistic to be informative (see Material and Methods). First, we explored the extent to which mobility differed between pre- and post-Last Glacial Maximum (LGM) hunter–gatherers (Fig. 3). We found the average (median) mobility rates to be higher ($\alpha = 18.1; 95\%$ CI: 14.9–87.7; $P = 0.08$) among pre-LGM hunter–gatherers, temporally ranging from 37,000–26,000 y ago, compared with post-LGM hunter–gatherers ($\alpha = 9.9; 95\%$ CI: 9.5–10.9; $P = 0.03$), temporally ranging from 19,000–5,000 y ago. We also estimated mobility rates for Holocene farmers, temporally ranging from 10,000–1,000 y ago, and found even higher values ($\alpha = 34.8; 95\%$ CI: 33.9–35.3; $P < 0.0001$) than for both hunter–gathering groups (see SI Appendix, Table S2 for full results).

Because Holocene western Eurasia is particularly well sampled for ancient genomic DNA, we performed a sliding window analysis to explore changes in mobility over the last 14,000 y in more detail (Fig. 4), using 4,000 y-wide windows to ensure sufficient temporal signal within each window. We inferred a reduction in mobility rate between 14,000 and 9,000 y ago, before the start of the Neolithic transition (Fig. 4A). However, throughout most of this period, the $P$ values are not significant (Fig. 4B). Because of the small sample size in the windows covering this time period (Fig. 4C), there is no significant correlation between genetic and temporal distances, and as a result,
Materials and Methods

When testing our estimator and the true mobility rate, we statisti- 
cally used a proxy for mobility because local 
inference can create confounding spatial or temporal population 
structures. However, this is a common problem for any analysis 
assuming neutral evolution and can be dealt with by focusing on 
putatively neutrally varying traits or loci.

The $S_{\text{max}}$ statistic offers a robust alternative to existing 
methods for the quantification of IBD patterns in temporally 
transporting heterogeneous datasets. In population genetics, correlations 
between trait differences and geographic distances are commonly 
used to infer past population structure and connectivity between 
populations (27). In such approaches, temporal structures in data 
are usually either ignored or mathematically controlled for 
by using partial least squares (e.g., ref. 28), but both of these practices 
have been criticized (29–31), and we show that while such 
approaches can inform the cumulative effects of migration in terms 
of structure reduction, they are unable to recover temporal 
changes in migratory activity. Partial least squares analysis 
assumes that the effect of time on genetic differences can be 
decoupled from the effect of space, which is generally not the case. 
We avoid this problem by integrating space and time into a 
single distance measure. Finally, because the statistic contains 
information about both spatial and temporal structuring of the 
populations, it can be used as a potentially informative summary 
statistic in quantitative model-fitting frameworks such as Approx- 
imate Bayesian Computation (32).

Using the $S_{\text{max}}$ statistic on ancient genomic data, we identified a 
sequence of changes in human mobility from the late Pleisto- 
cene to the Iron Age in western Eurasia. We find some support 
for reduced mobility in west Eurasian post-LGM hunter–gath- 
ers compared with pre-LGM populations. The reasons for this 
result are, as yet, unclear, although possible explanations include 
reduced resource availability in pre-LGM Western Eurasia, 
reaching larger foraging ranges compared with post-LGM condi- 
tions (33, 34) and/or residual post-LGM population structure 
following recolonization of northern latitudes from LGM southern

we do not observe any EC and so lack power to estimate mobility 
(see Materials and Methods and SI Appendix, Fig. S3). We con- 
sequently treat the inferred decline in mobility in this time range 
with caution. Second, we infer a substantial increase in mobility 
centered on the beginning of the Neolithic, with a peak centered 
around 7,500 y ago (Fig. 4A). Notably, the inferred mobility rate 
does not remain at this level throughout the Holocene. Instead, 
we infer a Late Neolithic drop in mobility before a second in- 
crease centered on the beginning of the Bronze Age, around 
5,000 y ago, then a decline in the Late Bronze Age and Early Iron 
Age, before a final increase centered on the Late Iron Age (Fig. 
4A and SI Appendix, Table S3 for full results for each window).

To validate the efficacy of our method to identify changes in 
migration rate on the time scales found in the empirical dataset 
(Fig. 4), we modified our simulations to represent a population 
experiencing two changes in migration rate, resulting in three 
episodes of constant migration rate. We observe a good corre- 
respondence between changes in $S_{\text{max}}$ and the simulated migration 
rate (SI Appendix, Fig. S4), supporting our interpretation of the 
empirical results in Fig. 4.

Finally, we compare the performance of the $S_{\text{max}}$ statistic to a 
simple IBD through time approach, where (the slope of) the 
linear relation between the genetic distances and geographic 
distances is used as an indicator of the level of past migratory 
activity: High levels of migration correspond to shallow IBD 
structures. However, this is a common problem for any analysis 
assuming neutral evolution and can be dealt with by focusing on 
putatively neutrally varying traits or loci.

Discussion

Through spatiotemporally explicit simulations, we have shown 
that the $S_{\text{max}}$ statistic can be used as a reliable proxy for the 
underlying relative mobility of individuals within a given time 
and geographic region. Because our statistic is based on 
correlations, it is well suited for analyzing data from archeo- 
ological and paleontological contexts, where preservation can vary 
significantly across different geographical areas and temporal 
ranges, and samples are commonly sparsely distributed across 
space and time. Nevertheless, in the extreme case of just a small 
number of sites from different geographic locations or temporal 
periods, spurious estimates of migratory activity may arise. The 
permutation procedure introduced in this study can be used to 
identify when the $S_{\text{max}}$ estimator is uninformative. We choose 
only to consider relative changes in the value of the $S_{\text{max}}$ esti- 
mator and do not attempt to interpret its values in absolute 
terms. This is because, while our intuition is that mutation rate 
and population size will not affect the relationship between ab- 
solute values of the $S_{\text{max}}$ estimator and the true mobility rate, we 
assume the possibility that other factors may. Selection in response 
to ecological and environmental factors could also reduce the 
utility of the $S_{\text{max}}$ statistic as a proxy for mobility because local 
selection can create confounding spatial or temporal population 
structures. However, this is a common problem for any analysis 
assuming neutral evolution and can be dealt with by focusing on
in trade and warfare during that period (43–45). Overall, our analysis suggests a strong link between technological change and human mobility in Holocene Western Eurasia. However, it should be noted that we have used wide windows (4,000 y), which necessarily reduces chronological resolution.

A major strength of our method is its applicability to any set of neutrally evolving heritable traits where differences between individuals can be quantified and increase monotonically with geographic distance and temporal difference. This means that, in principle, the $S_{\text{max}}$ statistics could allow the quantification of migratory activity in temporal and environmental contexts where obtaining ancient genetic data is not feasible, by using phenotypic data such as variation in cranial morphology, which has been shown to fit the pattern of neutral evolution and closely follow the patterns observed in analyses of neutral genetic data in humans (46, 47). Another exciting possibility is the quantification of movement based on cultural variation data, provided that appropriate near-neutral traits are used (e.g., refs. 48–50).

While it should not be assumed that the movement of artifacts always coincides with that of people, contrasting measures of movement based on genetics and cultural artifacts obtained under the same conceptual framework would allow quantification of demic vs. cultural diffusion processes. This might permit identification periods and regions where genetic, phenotypic, and cultural processes are coupled, or decoupled. Given its robustness and flexibility, we anticipate that the $S_{\text{max}}$ estimator will be applicable to a wide range of genetic, phenotypic, and cultural traits, allowing the quantification of mobility in a wide variety of scenarios in which this type of analysis has previously been challenging.

**Materials and Methods**

The proposed migration rate estimator, $S_{\text{max}}$, is the value of a scaling factor combining spatial and temporal distance matrices into a single distance matrix that maximizes its correlation with a matrix of trait distances. To estimate that value, the geographical, temporal, and trait distance matrices are calculated as described below.

**Geographic, Temporal, and Trait Distances.** The geographic distance between all sample pairs was calculated in kilometers using the Haversine Eq. (S1) to account for the curvature of the Earth as follows:

$$G_{ij} = 2 \arcsin \left( \sin \left( \frac{\phi_i - \phi_j}{2} \right) \sqrt{\cos(\phi_i) \cos(\phi_j) \sin \left( \frac{\lambda_i - \lambda_j}{2} \right)^2} \right),$$

where $G_{ij}$ is the distance in kilometers between individuals $i$ and $j$; $\phi_i$ and $\phi_j$ are the latitude coordinates of individuals $i$ and $j$, respectively; $\lambda_i$ and $\lambda_j$ are the longitude coordinates of individuals $i$ and $j$, respectively; and $r$ is the radius of the earth in kilometers.

Temporal distances between samples were calculated as time in years between sample pairs. Previously reported date ranges based on stratigraphy or direct radiocarbon dating were used for all individuals (SI Appendix, Table S1). In all analyses, sample dates were randomly drawn from a uniform distribution corresponding to the upper and lower bounds of a time period for a given specimen.

Genetic distances were calculated as pairwise proportion of alleles that are not identical by state (pairwise heterozygosity), using the function `ibs.dist` from the Bioconductor package SNPRelate v.1.18.0 (S2) in the R statistical analysis environment v.3.2.2 (S3).

**The $S_{\text{max}}$ Estimator.** To consider the full range of scaling factors on a finite interval, we choose to represent $S$ as the tangent of an angle $\alpha$ between $0^\circ$ and $90^\circ$, where $\alpha = 0$ corresponds to $S = 0$ (geographic variation alone explains the observed trait distances between entities) and $\alpha = \pi/2$ corresponds to $S = \infty$ (temporal variation alone explains the observed trait distances between entities). Formally, the time–space product matrix ($D$) was calculated as follows:

$$D_{i,j} = \sqrt{G_{ij}^2 + (ST_{ij})^2},$$

where $i$ and $j$ are the specimens considered, $D$ is the time–space product matrix, $G_{ij}$ is the geographical distance matrix, $T$ the temporal distance matrix (given by the difference in age of the samples), and $S$ is the scaling factor ($S = \tan(\alpha)$).
To find the scaling factor, $S_{\text{max}}$, that maximizes the correlation between the trait distance matrix and $D$, the time–space product matrix, we calculated the Pearson correlation coefficient between these matrices for 200 (500 for the simulated data) scaling factor values (Fig. 1). The scaling factor value in the time–space product matrix that produced the strongest correlation with the trait distance matrix is recorded as $S_{\text{max}}$, the mobility estimator.

**Simulation Tests.** The reliability and the robustness of the $S_{\text{max}}$ statistic in recovering information about past mobility was explored using a spatiotemporally explicit simulation model. The simulation world consists of a grid of 8,000 by 8,000 demes. Each simulation starts with one entity placed in a randomly chosen deme and lasts 20,000 generations. The model simulated exponential population growth to a carrying capacity of 10,000, entities, followed by a stochastic birth–death process (54) mobility, and trait mutation. We generated spatiotemporal trait variation data under different mobility parameter values using the same $S_{\text{max}}$ estimation protocols as described above for each dataset. A total of 10,000 independent replicates of the simulations and analyses were generated, and the utility of the $S_{\text{max}}$ statistic in recovering information about mobility was assessed by correlation.

The migratory process was modeled as Gaussian random walks: In each generation, each entity moves independently in the $x$ and $y$ directions by distances picked randomly from a normal distribution with mean $\mu = 0$ and SD $\sigma_{\text{mig}}$. This corresponds to the average distance moved in a single step (4) of $\sqrt{\pi}/2 \sigma_{\text{mig}}$; Thus, $\sigma_{\text{mig}}$ is the parameter of interest. We choose 1,000 random values of $\sigma_{\text{mig}}$ from a uniform distribution with a range of 1–100. We modeled drift as a Moran-type birth–death process (54). At each generation, each entity undergoes binary fission with probability $P = 0.1$, creating a duplicate of itself at the same location. The two entities subsequently move and evolve independent of each other. When the number of entities reaches or exceeds the carrying capacity (10,000), excess entities are deleted at random among all entities present in that generation. Mutation was modeled as a one-dimensional Gaussian random walk for each trait ($\mu_{\text{mig}} = 0$). Each trait was assigned an initial value of 1,000, and new (mutated) values were picked from a random normal distribution with mean equal to the current value and SD fixed at 0.05.

Following a burn-in period of 10,000 generations, entities were sampled from simulations with a probability of 0.0001 at each generation. The $x$ and $y$ coordinates, time of sampling in generations, and the values for the 50 traits were recorded for all sampled entities. Pairwise trait distances between all sampled entities in each of the simulated datasets were calculated using the Euclidean distance formula as follows:

$$M_{ij} = \sum_{k=1}^{n} (d_{ik} - d_{jk})^2,$$

where $M_{ij}$ is the distance between the two entities $i$ and $j$; $d_{ik}$ and $d_{jk}$ are the values of the trait $k$ for individuals $i$ and $j$ respectively; and $n$ is the number of recorded traits.

Out of 10,000 simulations, 9,866 (98.66%) resulted in an EC greater than zero. To match the simulated data with the empirical data, we filtered the simulated data based on the measured EC values and removed all simulations that produced an EC value smaller than 0.001. This resulted in 9,155 simulated data based on the measured EC values and removed all simulations that produced an EC value smaller than 0.001. This resulted in 9,155 simulated data based on the measured EC values and removed all simulations that produced an EC value smaller than 0.001.

**Confidence Intervals and Robustness of $S_{\text{max}}$ Estimator.** We tested the assumption that there is an IBD pattern by correlating the genetic (trait) distance matrices in all time bins and in all windows with the respective geographic distance matrices and the date-resampled temporal distance matrices and calculated the $P$ values for these correlations. We find a positive and statistically significant IBD pattern in space in all windows (SI Appendix, Fig. S3 A and B, respectively and SI Appendix, Fig. S6). The isolation by temporal distance pattern is positive and significant for most windows, but some windows show negative correlations or are not significant. We find that these windows correspond to time periods where we observe low EC (SI Appendix, Fig. S3C) and also low $P$ values for the EC (Fig. 4B).

To account for the uncertainty in sample ages, we calculated the scaling factor angle 10,000 times using dates resampled at random from a uniform distribution for each sample, as described above, and report the average of the scaling factor angle of the given distribution as a point estimate.

We also performed a leave-one-out analysis (10,000 replicates, combined with sample date resampling) to explore the combined effect of sampling and dating uncertainty and constructed approximate equal-tailed 95% confidence intervals for all groups and windows.

To assess the statistical significance of $S_{\text{max}}$ estimates, we consider the EC—defined as the Pearson correlation coefficient between the trait difference matrix and the time–space product matrix when $S = S_{\text{max}}$, minus the Pearson correlation coefficient between the trait difference matrix and either the temporal or geographical distance matrix alone, whichever is higher. To obtain a null-distribution of EC, we permuted trait data for individuals among the spatiotemporal sample locations 10,000 times and calculated EC for each permutation, as described above. Finally, we calculate the proportion of EC values from the permuted datasets that are equally high or higher than that obtained from the observed data. This permutation test permits assessment of how frequently the EC for the observed data are produced by chance alone or, alternatively, as the result of the method used for estimating the $S_{\text{max}}$ statistic. The resultant $P$ value is the probability of obtaining an equally high or higher EC value in permuted, supposedly signal-less data, and provides an indication of the information content of each dataset.

**Simulated Scenario of Changing Migration Rate.** We modified our simulations to represent a population experiencing two changes in migration rate, resulting in three episodes of constant migration rate. We assumed a generation time of 25 y and chose the effective population size to be $2N_e = 10,000$, standard figures in population genetic models of European populations (62). We next chose three levels of migration with relative magnitude on par with what was inferred from the empirical data: $m_1 = 0.0002$, $m_2 = 0.01$, and $m_3 = 0.05$. To ensure equilibrium conditions during the start of the sampling period, we discarded the first 10,000 steps of the simulation (using migration rate $m_1$). We then simulated a time period of 20,000 y, divided into three episodes with constant migration rate: $m_1$ for 25,000–15,000 y ago, $m_2$ for 15,000–10,000 y ago, and $m_3$ for the last 5,000 y of the simulation. This roughly corresponds to the time spans associated with Mesolithic hunter–gatherers, Neolithic farmers, and post-Neolithic cultures in our empirical dataset. From a population genetic point of view, whole genome data as used in the empirical estimates correspond to a large number of approximately independent replicates. Because our model does not include recombination, we accounted for this effect by increasing the sample size to 10,000 individuals. SI Appendix, Fig. S4 shows the migration rate estimation using the $S_{\text{max}}$ statistic using a 4,000 y-wide sliding window. R version 3.2.2 (53) was used for analyses throughout this manuscript. The correlations between temporal, geographic, and trait distance matrices were calculated using the mantel (method = “pearson”) function in R package Vegan version 2.3.0 (63). The permutation and bootstrap tests were performed using the function sample in the R package base version 3.2.2 (53).
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