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Three-Dimensional-Printable Thermoactive Helical Interface with Decentralized Morphological Stiffness Control for Continuum Manipulators

S.M.Hadi Sadati¹,²,³, Luis Sullivan², Ian D. Walker⁴, Kaspar Althoefer⁵ and Thrishantha Nanayakkara³

Abstract—We present a 3D-printable thermoactive scale jamming interface as a new way to control a continuum manipulator dexterity by taking inspiration from the helical arrangement of fish scales. A highly articulated helical interface is 3D-printed with thermoactive functionally graded joints using a conventional 3D printing device that utilizes UV curable acrylic plastic and hydroxylated wax as the primary and supporting material. The joint compliance is controlled by regulating wax temperature in phase transition. Empirical feed-forward control relations are identified through comprehensive study of the wax melting profile and actuation scenarios for different shaft designs to achieve desirable repeatability and response time. A decentralized control approach is employed by relating the mathematical terms of the Cosserat beam method to their morphological counterparts in which the manipulator local anisotropic stiffness is controlled based on the local stress and strain information. As a result, a minimalistic central controller is designed in which the joints’ thermo-mechanical states are observed using a morphological observer, an external fully monitored replica of the observed system with the same inputs. Preliminary results for passive shape adaptation, geometrical disturbance rejection and task space anisotropic stiffness control are reported by integrating the interface on a continuum manipulator.

Index Terms—Flexible Robots, Compliance and Impedance Control, Medical Robots and Systems.

I. INTRODUCTION

PERFORMING complicated tasks such as manipulation in unpredictable conditions, where safe interaction with the environment is important, requires dexterity and compliance.

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Fig. 1. (a) Overlapping and helical arrangement of scales in a Cyprinus Carpio fish, (b) the thermoactive interface integrated on a two module STIFF-FLOP continuum manipulator for stiffness control (left & middle) and shape locking (left & right) in the straight and bent configurations. in which low actuation energy, high dexterity, reachability, maneuverability, back drivability and self-adjustability of continuum mechanisms have proven to be advantageous. However, compliance has disadvantages such as uncertain deformations, limited control feedback, reduced control bandwidth, stability issues and underdamped modes where high stiffness and damping modes are required to achieve precision in tasks involving working against external loads [1], [2]. As a biological solution, natural skin, especially with scales as flexible armor in animals such as fish, turtles, armadillos and snakes, show stiffness regulation in response to irritation or penetrating forces. The scales slide almost freely in general movements, but are jammed as a result of penetration forces while the overlapping area increases due to inward bending of the skin to provide even more protection [3]. However, the role of passive or active scale jamming on the animal body stiffness regulation has not yet been addressed adequately.

Jamming as a means for stiffness control, by modulating the shear forces due to Coulomb and viscous damping between the jammed and interlocking media, has been utilized in design of variable stiffness manipulators [4], [5], [6] of which a comparative study by Wall shows the advantages of a layer jamming arrangement [7]. Tendon-driven jamming is introduced recently to overcome controllability and portability limitations of vacuum enabled jamming in underwater and space applications [8], [9]. The jamming media behaves similarly to a ductile material that undergoes an elastic followed by a plastic deformation in which the elastic deformation threshold (yield) is a function of the friction between the jamming media controlled by the normal force on the contacting surfaces. A high hysteresis is a result of this behavior and the external load should be kept below the yield threshold for an almost linear and repeatable behavior. This behavior is similar to the stiffness change due to phase and glass transition in
low melting point (LMP) alloys, such as field’s metal [10], [11], and composite material with inherent thermal instability, such as wax [12] and ABS [13]. This class of material is used in much recent research due to higher stiffness range (4.65-5.76 times increase in the stiffness [13]), easy electrical modulation through heating, self-healing properties and 3D printable fabrication compared to other stiffening mechanisms [1], [10]. However, the thermoactive design suffers from slow response time in the cooling process, poor controllability and repeatability due to complex phase transition, low efficiency due to heat dissipation, sensitivity to ambient temperature and safety issues due to high current and temperature which are not adequately addressed in recent studies [1], [12], [13], [11]. These should be addressed with proper structure and control design and implementation of a cooling mechanism based on the final application. Thermoactive materials are more suitable for applications in cold ambient temperature where rapid cooling improves the system response time and repeatability, e.g. underwater [14], space and high attitudes [15], [16], and for static tasks, e.g. shape locking for continuum manipulators [6] and robotic surgeries with mostly quasi-static operations [1], [2], [5], [11]. A recent review of stiffening solutions for continuum manipulators by Blanc, et. al. shows the advantages of shape locking mechanisms to achieve higher stiffness values and low melting point material for higher stiffening ratio [1].

Planning and control of stiffness reconfigurable mechanisms require cumbersome analytical and computation tools for which the idea of exploiting the embodied intelligence or morphological computation of the available physical hardware has been introduced [17], [18]. By breaking a complex control problem into simple sub-problems, a decentralized control system is formed that benefits from parallel execution and lack of communication delay where the tasks are fulfilled based on simple repetitive actions with limited local sensory feedback and computation capabilities [19].

In our previous work, we presented a tendon-driven interlocking scale jamming design inspired by the helical arrangement and morphology of the fish scales (Fig. 1.a) to control torsional stiffness of a helical interface cross-section. As a result, we achieved a simpler design and actuation method which, for the first time, provides better wearability, linear behavior and lower hysteresis as well as high load-bearing capacity and linear stretch in uniform actuation [9] compared to the previous locking and jamming designs [1]. It should be noted that biomimicry is not the objective of this study. Rather, we aim to test the hypothesis that contact friction/locking control using scales is a viable method for stiffness control of exoskeletons for soft robots. However, such design may be useful to uncover or test hypotheses about the operation of biological structures [14], [17], [19]. While usually the jammed surfaces normal force is controlled for stiffening, recently, we investigated the idea of using a novel thermoactive shape memory Velcro mechanism between the layers [20].

To achieve higher load-bearing range, simpler actuation mechanism, smaller setup design and, most importantly, local anisotropic control over the stiffness tensor, in this paper, we investigate how the inter-scale elasticity and damping for the same helical interface can be controlled by phase transition temperature control of an LMP composite wax in a 3D-printable functionally graded thermoactive joint design. As a result, our design benefits from the advantages of an interlocking design and using low melting point material. First, a design overview is presented in section II. A new two-step mathematical model is proposed in section III. The manipulator mechanics is modeled with variable curvature (VC) kinematics via the Cosserat beam method [21] and the stiffness tensor of the rounds of scales in each element is found using the Principle of Virtual Work (PVW). Mean values for an element elastic coefficient are found based on the joints’ elastic and plastic deformations. A decentralized morphological controller is introduced in section IV to simplify the problem of shape adaptation and stiffness regulation in response to external geometrical disturbances. The novel idea of morphological observer is introduced, where the system states are estimated based on the measurements from an external fully monitored joint with the same design and control signal. The repeatable characteristics of such joints are investigated based on the phase transition profile of the LMP hydroxylated wax and for different joint designs and actuation scenarios, and experimental relations are identified to implement forward control of such joints in section V. In section VI, experiments are carried out to investigate the performance of the modeling and forward control for the interface uniform and anisotropic stiffness regulation while the states are observed with the morphological observer. Finally, the proposed decentralized controller is briefly tested for shape adaptation and task space stiffness regulation in presence of geometrical disturbances. Supplementary video and explanation files about the experiments are provided too.

II. 3D-PRINTABLE THERMOACTIVE INTERFACE

UV curable Thermally stable acrylic plastic (elasticity modulus, $E = 3.2$ [GPa]) and low melting point hydroxylated wax (melting point of 55-65 [°C]) are widely used in high definition 3D printing as the main and the supporting material, where the support material is removed in an oven or hot water after the process. A helical interface with single-axis revolute joints is designed (Fig. 2.a,b) to be printed as a whole unit (Fig. 2.c). A small empty space is left in the joint which is filled with the wax support material in the printing process and small clearances of 0.15 [mm] in diameter and length are considered for free rotation of the joints while preventing the wax from escaping. Four non-contacting teeth with 0.6 [mm] height are designed to increase the joint surfaces engagement with the wax. Based on the von Mises yield criterion, the tooth
surface should be larger than 0.58 times the shear surface, so the material withstands the teeth bearing force before the shear sliding begins. A spiral path with 7.9 [mm] groove diameter and two small hinges hold three rounds of heating wire with length \(l = 7.45\) [mm] in place (Fig. 2.b). The fully assembled interface is printed as a complete unit with a commercially available high definition 3D printer (PROJET HD 3000 Plus from 3D Systems, www.3dsystems.com) without any further modification to the printer. The interface is ready to be used straight away after addition of the heating Nichrome wires (nickel(80%)-chrome(20%) alloy wire, 0.1 [mm] diameter, resistance \(R \approx 1\) [\(\Omega/cm\)], from rapidonline.com). The wax is fully jammed when cooled and becomes a lubricant when melted, providing high range of stiffness variability through temperature regulation with small electric actuation. As a result of the small joint design, the small amount of wax forms a thin layer that facilitates heat conductivity and improves stiffness regulation repeatability and response time, while high-performance heating wires are used for efficient temperature control compared to high current (3-5 [A]) Joule heating method in similar research [11]. A 120 [deg] scale curve is suitable for stiffness regulation along the actuation lines of continuum actuators with three pressure chambers, e.g. STIFF-FLOP [2] (Fig. 2.a), a 90 [deg] curve provides decoupled stiffness control in the Cartesian task space (1.b) and a 135 [deg] curve is suitable for a long interface design with smaller number of joints (Fig. 2.c).

III. MODELING FRAMEWORK

Local stiffness regulation along a continuum manipulator backbone enables simultaneous task space impedance and configuration control as well as disturbance rejection. We assume that each full helix turn adjusts the stiffness coefficient matrices of an element (\(K_v\) and \(K_u\)) along the manipulator backbone by selective actuation of stiffness controllable joints (Fig. 3.a). The PVW and Castiglione’s method are used to find \(K_v,u\) to be used in the Cosserat rod method describing the manipulator mechanics.

A. Backbone Variable Curvature Mechanics

We use beam theory (Cosserat rod) method as in [22],

\[
\begin{align*}
\rho,s &= R(v + [0, 1, 0]^T), \quad R_u = [u] x R \\
v &= K_v^{-1}, (R^T, (f_b + f_u) + f_p) \\
u &= K_u^{-1}, (R^T, (\tau_b + \tau_u) + \tau_p),
\end{align*}
\]

where subscript \((.,.)\) means partial differentiation w.r.t. variable \(x, s \in [0, l]\) is the axial position, \(l\) is the backbone initial length, \([d_2, d_1, d_3]\) are local curvilinear frame directions, \(v\) is the vector of linear strains and \(u\) is the vector of curvatures and torsion in the local curvilinear frame, \(R\) relates \(\epsilon = [v, u]\) to the manipulator Cartesian \((\hat{i}, \hat{j}, \hat{k})\) geometry (\(\rho\), \([\ ]\_x\) is an operator to create a skew symmetric matrix, \(f_p\) and \(\tau_p\) are the actuator loads, \(f_b = (l - s)\sigma a_i g_j\) is the body weight load, \(\tau_b = \sigma a_i g_j \hat{e} \times g_j\) is the body weight moment, \(\tau_u = (\rho(s) - \rho(c)) \times f_u\) is the moment of the external load exerting at \(s = s_L\), \(a_i = \pi R^2\) is the module cross-section area with radius \(r_c\) and \(\sigma\) is the material density.

B. Helical Interface Kinematics

Assuming no axial twist, for the geometry of a helix \(\rho_h\) with variable curvature backbone we have \(\rho_h = R(2, \varphi, [r_h, 0, 0]^T), \varphi = 2\pi n/m,\) where \(R(\varphi)\) is a rotation matrix of \(\varphi\) around the \(i^{th}\) axis, \(n_h\) is the number of helix turns, \(l\) is the backbone initial length and subscript \((,)_h\) is for the helix parameters [22].

C. Helical Interface Stiffness Model

The load-deformation plot for jamming media usually consists of an elastic followed by a plastic deformation with two distinctive stiffness coefficients (slopes of the \(f - \Delta l\) curve in Fig. 2.d), \(k_E\) for the fully jammed state (elastic region) and \(k_p\) for when the jammed media begins to slide (plastic region) resulting in stiffness discontinuity, where \(f = [n, m], n\) is linear force and \(m\) is moment. Here, \(k_E,P\) are functions of the material temperature and density. For the first time, we introduce an equivalent stiffness as in Fig. 2.d for continuous stiffness modulation with such design as the ratio of external load to the summation of elastic and plastic deformation. We assume infinite shear, a valid assumption for relatively long continuum manipulators where there is no deformation due to torsion \((m_{d_1} \approx 0)\) and shear forces \((n_{d_2} = n_{d_3} \approx 0)\) on the manipulator cross-section. Local helix lead angle is assumed to be almost perpendicular \((\gamma \approx \pi/2)\) and hence constant [21], [22] and its effects are neglected. Based on the free body diagram (Fig. 3.a), we have \(m_h = R(2, \varphi), ([r_h, 0, 0] \times n + m)\) for the moment in the helix curvilinear frame, where \(m\) and \(n\) are moment and force, \(r_h\) is the helix mean radius, \(\varphi\) is the polar angle around \(d_3\) axis and \(C[S] = \cos\sin (z)\). The scale body and the joint act as series elastic elements. Using the PVW, the differential virtual work for the \(i^{th}\) scale in each element \((dw_{sec})\) is

\[
\begin{align*}
w_{sec} &= \int_{\phi}^{\phi_i} dw_{sec}, \quad \phi_i = 2\pi n / n_{sec}, \quad (2) \\
dw_{sec} &= (m_h \varphi_i/(2EJ_3) + (m_{h_1} + \tau_{y})^2/(2EJ_4))r_h d\varphi,
\end{align*}
\]
where \( n_{sc} \) is the number of scales or joints in a full turn, \( \tau_y \) is the yield resistance torque of the \( i \)th joint, \( E \) is the module of elasticity and \( J_i \) is the scale second moment of area around the \( i \) principle axis. For the \( i \)th joint we have

\[
\begin{align*}
K_{vi} &= \frac{(m_{hi}(\varphi_i) + \tau_y)}{2k_E}, \quad w_{Ei} = \frac{(m_{hi}(\varphi_i) + \tau_y)^2}{2k_E}, \\
K_{vi} &= \frac{\tau_y(m_{hi}(\varphi_i) - \tau_y)}{k_p}, \quad w_{P_i} = \frac{(m_{hi}(\varphi_i) - \tau_y)^2}{2k_p}, \quad w_{\mu_i} = \frac{\tau_y(m_{hi}(\varphi_i) - \tau_y)}{k_p},
\end{align*}
\]

where \( w_{Ei} \) is the virtual work for the elastic deformation, \( w_{P_i} \) is the virtual work for the plastic deformation and \( w_{\mu_i} \) is the virtual energy dissipated by the joint friction. The total energy of each element is \( w = \sum_{i=1}^{n_{sc}} (w_{Ei} + w_{P_i} + w_{\mu_i}) \). For the equivalent stiffness of the element \( (K_{vi}) \) using Castigliano’s method, we have \( v = w_{Ei}, u = w_{\mu_i} \), and

\[
K_v = \text{diag}^{-1}(v), \quad K_u = \text{diag}^{-1}(u), \quad m = \frac{v}{u}, \quad n = \frac{u}{v}, \quad K_v = \text{diag}^{-1}(v), \quad K_u = \text{diag}^{-1}(u), \quad m = \frac{v}{u}, \quad n = \frac{u}{v},
\]

where \( v, u \) and \( K \) are functions of \( \tau_y \) and \( f = [n, m] \), and for each scale we have the following piecewise rule.

- **Elastic region** \( (m_{hi}(\varphi_i) \leq \tau_y, \quad v_i = 0) \): the terms resulting from \( w_{P_i}, n, m \) and \( w_{\mu_i} \) are neglected, and \( \tau_y = 0 \) in all other terms.
- **Plastic region** \( (m_{hi}(\varphi_i) \geq \tau_y, \quad \|v_i\| = 0) \): \( [n, m] = 0 \) in the terms resulting from \( w_{Ei}, n, m \) and \( w_{sc}, n, m \).

\( v \) is relative velocity of the surfaces in plastic deformation.

Eq. (4) is rearranged to find \( \tau_y(f, \varepsilon) \) and \( \tau_y(f, K) \) for stiffness planning and control. The resulting equations for \( \tau_y \) are not independent, since the scales are in series with each other, and the axial and the bending stiffness cannot be controlled simultaneously. Using the symmetry in a formation with four scales in each turn, the element axial stiffness is controlled by \( \tau_y = \tau_y(f, k_{ax}) \) and for the bending stiffness control we have \( \tau_y = \tau_y(f, k_{ax}) \) and \( \tau_y = \tau_y(f, k_{ax}) \). Then, we have \( K_v = K_v(f, \tau_y) \) to be used in Eq. (1).

### IV. Morphological Control and Observation

#### A. Shape Adaptation and Configuration Control

The interface is fully compliant during manipulations featuring passive shape adaptation (Fig. 1.b middle) and can lock any final shape (Fig. 1.b right). A larger reachable configuration space is possible with minimal control inputs and local stiffening of the interface.

#### B. Decentralized Morphological Control

A model-based decentralized morphological controller is proposed to simplify the complex problem of impedance disturbance rejection at any point along the backbone.

1) **Model-Based Control:** A simple control law maintains a bias or desired stress by changing local stiffness that can be used for shape adaptation, disturbance isolation and task space impedance control. Local strains \( (\varepsilon) \) are assumed to be known to the local controllers of each element while the stress \( (\sigma) \), distributed along the manipulator, is considered as a morphological signal conveying necessary information between the elements. Any impedance disturbance, e.g. contacting with soft or rigid environment, is canceled through proper shape adaptation. This does not include the case of constant external load. It means that the final disturbed strains \( (\varepsilon_e) \) are known and the goal is to maintain a desired contact force \( (f_d) \) for task space impedance control or impedance disturbance isolation by maintaining a bias force distribution similar to before the disturbance \( f_0 = K_{e0}, \) where \( e_0 \) is the initial strain before the disturbance. The stiffness for the element at the contact point is found from \( \tau_y(f, \varepsilon_e) \) (Fig. 3.c). The stiffness of the adjacent elements are adjusted to maintain the bias load distribution of the undisturbed structure \( (f_0) \) with the disturbed configuration \( (\varepsilon_e) \) using \( \tau_y(f_0, \varepsilon_e) \) (Fig. 3.c). As a result, the local disturbance is isolated and no change in the rest of elements are necessary (Fig. 3.c). The interface is looked in the new configuration.

2) **Simple Switching Control:** The contacting and adjacent elements are fully softened to reach \( f_d \) through passive shape adaptation and then are solidified.

#### C. Minimal Central Controller

1) **Central Controller Design:** A simple central controller, as in Fig. 4, can be designed based on the proposed decentralized control paradigm, where a switching relay unit connects a single current controller unit to each of the joints one at a time to regulate their temperature and stiffness with a time period less than the system response time. The manipulator geometry \( (\rho \text{ and } R) \) is found by interpolating a polynomial through tracked points along the manipulator, using magnetic tracking sensors [21], based on which the elements’ load distribution \( (f = [n, m]) \) and \( \varepsilon \) are observed using Eq. (1).

2) **Joint Morphological Observer:** Empirical feed-forward relations are used to control the joint yield torque \( (\tau_y) \) and temperature \( (T) \). However, these values cannot be measured directly to implement a feedback controller due to the large number of joints, sensor size and space limitation. The concept of morphological observer is thus introduced, which is a fully monitored replica of the observed system with the same inputs. Similar to a conventional observer where a computer model
is used to estimate inaccessible states, here we use a physical model for state estimation. An exactly similar joint with all the necessary sensors is designed (Fig. 5.f) and equivalent currents are supplied to the observed joint and replica. The system yield torque ($\tau_y$) and temperature ($T$) are estimated and controlled based on the morphological observer readings. However, the observation accuracy is prone to difference in working condition of the replica and observed system, e.g. orientation and ambient temperature.

V. SYSTEM THERMO-MECHANICAL PROPERTIES

High-performance Nichrome wire is used as a robust low current and efficient heating element. The wire resistance is found to be $R \approx 1[\Omega/cm]$ with time constant, the time that a thermistor temperature is dropped by 63.2%, equal to 8.1 [s]. A Maxon Motors EPOS2 5/50 is used for current control of the heating wire. Initially, a simple switching (Bang-Bang) controller is used to regulate the system mean temperature. The temperature is measured using a K-type thermocouple and a National Instruments NI-DAQmx 6210 for signal amplification, noise canceling and analog to digital conversion. A HIWIN KKA40 precision linear actuator unit is used for accurate linear displacement and an ATI-Nano17 6-axis force sensor is used to measure the loads in quasi-static condition.

A. Wax Melting Temperature and Pattern

The melting pattern, surface friction and shear stress of the hydroxylated wax support material are investigated. A cylinder (20 [mm] inner diameter and 20 [mm] height) is filled with the hydroxylated wax while heated with a 0.3 [mm] diameter spiral Nichrome wire at the center passing a 200 [mA] current. The thermocouple tip is placed in the middle (10 [mm] height) and with 4 [mm] radial distance from the inner surface. The support material had a cream color in the solid state. The melting starts around the heating wire while the material color turns to brown. The wax state starts at $\approx 40 [\degree C]$ and stabilizes at $\approx 45 [\degree C]$. The melting starts at $\approx 55 [\degree C]$ propagating from the vicinity of the heating spiral from top to bottom, due to natural heat convection in the melted wax, and stabilizes in $\approx 65 [\degree C]$ until the whole material is fully melted in about $\approx 6$ minutes. While cooled, the solidification starts at $\approx 55 [\degree C]$, trapping the air bubbles in the material, from the outer surfaces and completed in $\approx 22$ minutes with free air cooling and in $\approx 11$ minutes in water, both at room temperature ($T_0 = 26 [\degree C]$). Small heat conductivity of the wax results in a slow nonuniform transition pattern with visible borders (Fig. 5.a). While a large transition state is preferable for continuous stiffness control, compared to rapid melting of most LMP alloys [10], [11], a small enclosed volume should be designed to achieve uniform and fast response actuation.

B. Wax Shear Strength, Surface Friction and Stiffness

The same cylinder is covered with a cap and two shaft designs, a smooth cylinder to measure the resisting torque ($\tau$) and shear stress ($\sigma_{\text{shear}}$) due to surface friction, and a toothed design to calculate the same values for the material yield stress (Fig. 5.b). The effective radius, where the breaking starts, is 5 [mm], similar to the shafts’ base radius and $h_w = 12$ [mm] is the shaft active height The heating wire is placed on the joint outer surface where the melting starts. While precise high-resolution temperature regulation of the joint is possible, a step change of 10 [\degree C] is used in the experiments considering our real application with a smaller joint design. The temperature is not measured at the effective radius and is used only for comparison purpose. The yield and breaking values for the wax rigid state ($T < 40 [\degree C]$) is not reported due to force sensor saturation and damage to the joint structure. These values are reported for the final smaller joint design. Three full cycles of actuation are carried out in each experimental trial (Fig. 5.e). The material behaved like a brittle material in the first actuation cycle, where the resisting force sharply

![Image](image_url)
drops (Fig. 5.c 1st Break/Yield and Fig. 5.e), but more like a ductile material for the next cycles with distinctive yield point, where the plastic deformation begins (Fig. 5.c Mean Yield and Fig. 5.e), and breaking point, where the resisting force drops (Fig. 5.c Mean Break). The breaking torque is higher for the first cycle especially for the cylindrical shaft (≈%71) while in the toothed design this value is (≈%9). The mean yield strength of the toothed design is 4.5 times higher than the smooth cylindrical one showing higher shear stress strength compared to the surface viscosity and friction between the joint shaft and the wax. Variation of the material mean yield stress is noticeable, 8-500 [KPa] for the toothed design and 1-180 [KPa] for the cylindrical design, with a relatively sharp drop at the wax transition temperature especially for the cylindrical shaft. To identify the wax shear modulus \( G_w \), we considered the resisting torque for a small (1 [mm]=1.16 [rad]) deformation assuming: 1) the wax is fully rigid at the room temperature and the initial measured elasticity is only due to the joint structure \( k_{js} \), 2) the structure elasticity does not change with temperature. For \( G_w \) (Fig. 5.d) we have \( 1/k_j = 1/k_{js} + h_w/(G_wJ_w) \), where \( k_j \) is the joint measured stiffness, \( J_w \approx 3e^{-7} [m^4] \) is the wax cross-section second moment of area and \( h_w = 12 [mm] \) is the wax height.

The joint has a complex behavior with linear elastic stiffness in the first cycle but an increasing value for the later cycles (Fig. 5.e). While the yield strength of the 2nd and 3rd cycles are almost equal, the transition is delayed with an offset, especially in lower temperatures, resulting in a different equivalent stiffness. This is due to the wax melting pattern, self-healing properties and its porous structure variable density. The non-smooth stick-and-slip behavior in the wax state (plastic deformation) results in large hysteresis in a full actuation cycle and poor repeatability at the wax transition temperature for continuous operations. To achieve better repeatability and response time, we continue with a small toothed design and the characteristics of the first actuation cycle is used for the controller design. It is better stiffness range, linear behavior and a smoother stiffness-temperature profile. Besides, a small enclosed wax volume is considered to reduce the variability of the wax properties at the transition temperature (Fig. 5.f).

### C. A Single Joint Electro-Thermo-Mechanical Relation

A joint, as explained in section II (Fig. 2.b), is fabricated with a handle and a temperature sensor at the joint center (Fig. 5.f). The measured temperature at the joint center does not represent the wax temperature and the properties of the whole system are identified in this section. A similar test setup as in Fig. 5.b and a switching control are used. Empirical relations for mean values of current-temperature \((I - T)\), temperature-yield torque \((T - \tau_y)\) and temperature-elastic and plastic stiffness \((T - k_{E[P]}\) are identified to be used for feed-forward control. The mean heat capacity coefficient of the system is found to be 0.45 [J/°C] from the nearly linear initial heating stage of the temperature control experiments (Fig. 5.g). It takes 70 [s] to melt (50 [°C]) and 120-240 [s] to solidify the wax, 6-12 times faster than the bulky setup in section V-B, with ≈14.5 [s] lag between the current actuation and the temperature increase, almost independent of the temperature, due to the material low thermal conductivity. For \((I - T)\) relation we have (Fig. 5.h)

\[
T = C_11.235 \ e^{24.41T} + T_0, \tag{5}
\]

where \( C_1 \) is a correction factor, mainly due to the change in the heat dissipation coefficient, to be set before each run and based on a measurement with the morphological observer. The temperature variation is significant using a switching controller due to the system large thermal response time and inertia. A 5-6 times higher resistance torque for the first actuation cycle, a small drop (≈20-25%) for the next cycles and an offset in the initial position due to the system hysteresis are observed as in the previous section. The breaking point of the first cycle is considered for the control design (Fig. 5.i). Three temperature regulation strategies are tested: 1) heating, where the desired temperature is higher than the current temperature, 2) cooling, where the desired temperature is lower, 3) healing, where the wax is fully melted at 50 [°C] then cooled (healed) to the desired temperature. \( \tau_y \) varies based on the initial \( T \) for the heating and cooling strategies where continuous control is possible. The cracks, remained from previous tests, results in an undesirable drop in \( \tau_y \) in the cooling strategy (Fig. 5.i). The healing process provides higher \( \tau_y \) and smoother \( T - \tau_y \) relation; however, it needs to be executed either very quickly or when the interface is not loaded. We continue with heating strategy for continuous actuation and healing strategy for static scenarios or when the temperature is reduced. \( \tau_y \) is identified as

\[
\tau_{yheat} = 10.69e^{-0.251T}, \ \tau_{yheal} = 764.1e^{-0.3518T}. \tag{6}
\]

The small joint design results in an almost constant and repeatable stiffness during the tests and a smooth variation w.r.t. \( T \). \( k_{E[P]} \) for the joint are identified as (Fig. 5.j)

\[
\begin{align*}
  k_{Eheat} &= 9.017e^{-0.06715T} , \ k_{Pheat} = 2.328e^{-0.08929T}, \tag{7} \\
  k_{Eheal} &= 27.37e^{-0.09533T} , \ k_{Pheal} = 12.83e^{-0.1295T} .
\end{align*}
\]

Eq. (5-7) are used for feed-forward control, to minimize the temperature variation seen in Fig. 5.g,h, while a switching controller is used to compensate any feedback error.

### VI. INTERFACE EXPERIMENTS AND INTEGRATION

#### A. Model-Based Observation and Control

The model-based observation and control method is used for uniform axial and bending stiffness control of a helical interface sample with 3.5 active turns and 120 [deg] scales \( J_3 = 6.3e^{-11} , J_1 = 2J_3 \) from an initially straight position (Fig. 6.a,b). The control setup in Fig. 4 is used where the current control unit is connected to the common input of an Arduino relay shield controlled by an Arduino Uno SMD Rev3 board. Each relay is connected to a morphological observer and a row of joints, in the same ambient. A HIWIN precision actuator and an ACTUONIX L12 linear actuator (www.robotshop.com) with 10 [mm] stroke are used for axial and bending tests respectively. Three measurements, each with three deformation cycles are carried on for each experiment. All the joints are activated with the same current in the axial
The bending case has inactive locked joints at the 0 [deg], and a nine-turn helical interface with 90 [deg] scales (scale) for a 9 [mm] tip lateral deflection in straight (I) and bent (C) configuration (N: manipulator) and a nine-turn helical interface with 90 [deg] scales (scale) for a 9 [mm] tip lateral deflection in straight (I) and bent (C) configuration (N: manipulator, P: pressurized, R: rigid, S: soft), (b) passive shape adaptation.

The bending case has inactive locked joints at the 0 [deg], and a nine-turn helical interface with 90 [deg] scales (scale) for a 9 [mm] tip lateral deflection in straight (I) and bent (C) configuration (N: manipulator) and a nine-turn helical interface with 90 [deg] scales (scale) for a 9 [mm] tip lateral deflection in straight (I) and bent (C) configuration (N: manipulator, P: pressurized, R: rigid, S: soft), (b) passive shape adaptation.

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better scalability, due to omitting tendon routing friction, and local and directional stiffness controllability, the presented design benefits from high load-bearing to weight ratio, axial stretch and simple integration similar to our previous tendon-driven interface [9], but presents lower stiffness increase (straight: 83%, bent: 330%), due to the contribution of the tendon stiffness, and suffers from higher hysteresis, nonlinear behavior and lower repeatability. We plan to address these issues by an improved design based on a detailed heat transfer analysis, passing the interface through a helical tube filled with a coolant fluid, proper isolation of the heating wires, using multiple parallel helical strands and changing the scale dimensions for better shape locking and stiffness range.

C. Simple Switching Control

The proposed simple switching controller is successfully used for passive shape adaptation (Fig. 7.b), tip force regulation and isolation (Fig. 8 left), and backbone impedance disturbance isolation (Fig. 8 right) of the helical interface. The stiffness of the three elements along the interface is controlled separately. The simple control method increases the adjacent elements compliance to cancel the external load and isolate its effects through passive shape adaptation. 50% of the configuration at the element borders and 92% of the external force in the tip disturbance case and 33% of the configuration and 91% of the external force in the backbone disturbance case are canceled in less than 90 [s]; however, the recovery is limited due to the system passive shape adaptation.

VII. Conclusion

A thermoactive scale jamming interface is 3D-printed with a commercially available device as both a new way to control a continuum manipulator dexterity and a method to fabricate general mechanisms with thermoactive functionally graded designs. The interface compliance is regulated by controlling the joints’ wax temperature for which empirical relations are identified. The common problems of poor repeatability and response time with low melting point material are addressed with a small wax enclosure design and using empirical relations in the controller design. Novel morphological observation and decentralized control approaches are employed based on which a minimal central controller is implemented. Preliminary results for passive shape adaptation, geometrical disturbance rejection and task space anisotropic stiffness regulation are presented by integration of the interface on a continuum manipulator. Our results show potential of our platform and method for stiffness planing of continuum manipulators, especially for quasi-static operations in cold environments such as underwater and space.

REFERENCES


